



# Recent HEP.TrkX results

Xiangyang Ju, Steve Farrell

Exa-TrkX kick-off meeting, 4 June 2019

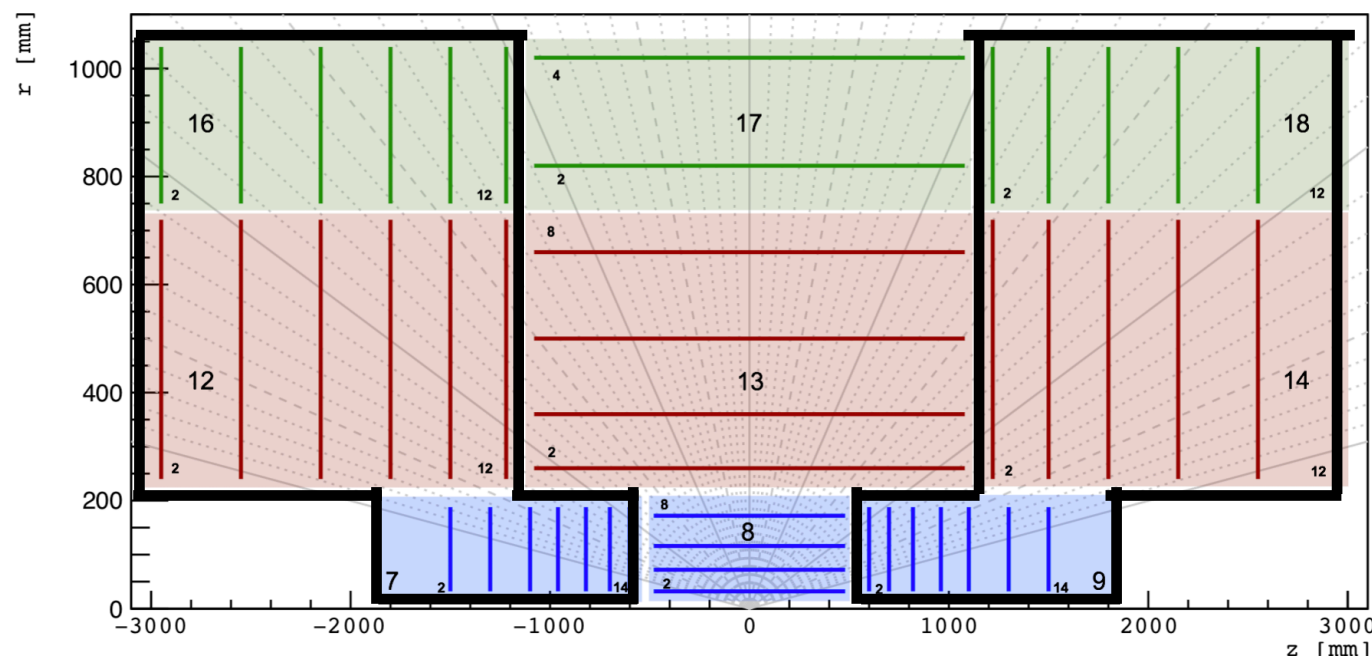
# Introduction

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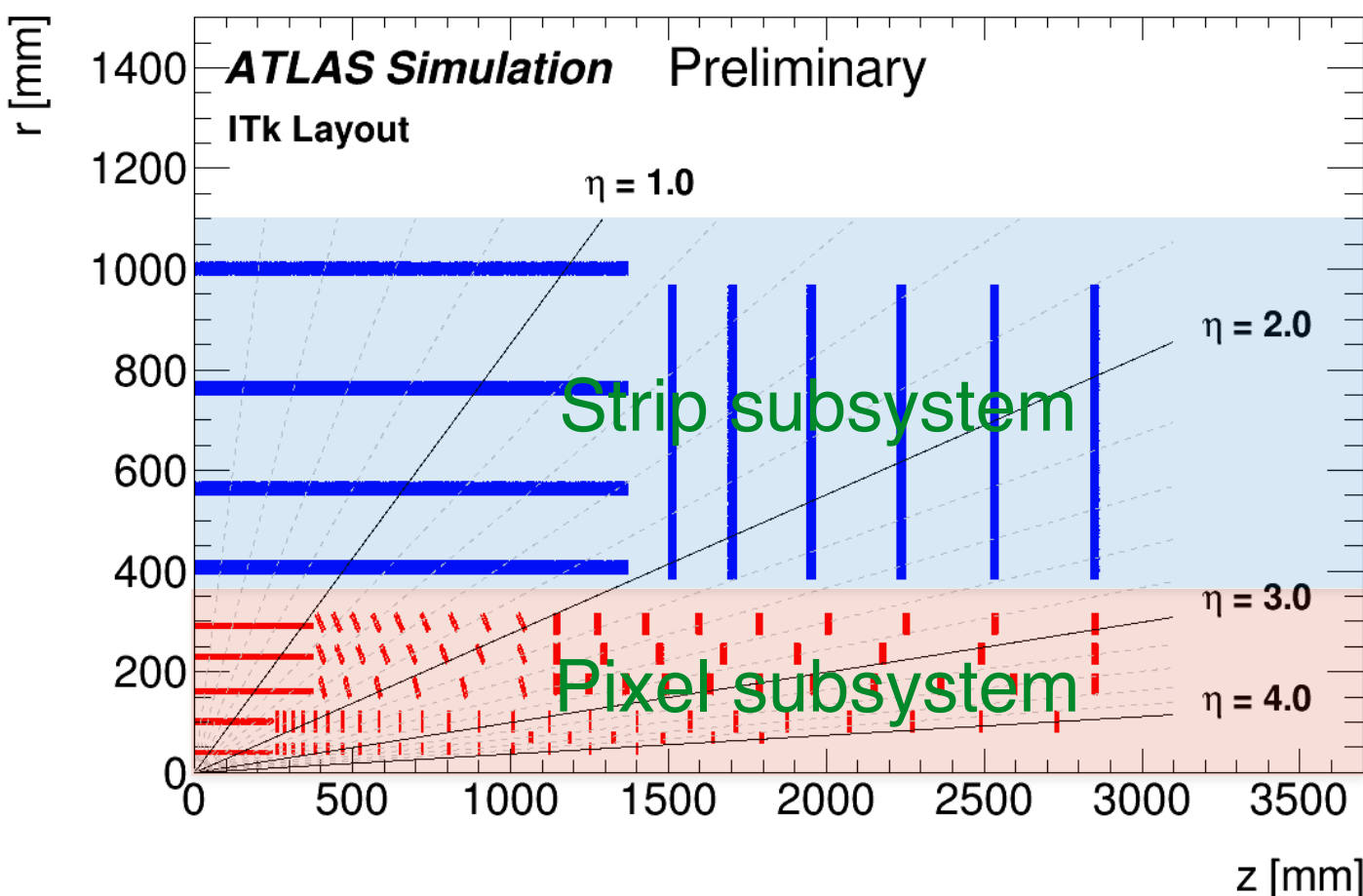
1. Recap the results presented at the 2019 Connecting The Dots
2. Recent results after that
3. Future plans

# Tracking ML challenge data

[[link to the website](#)]

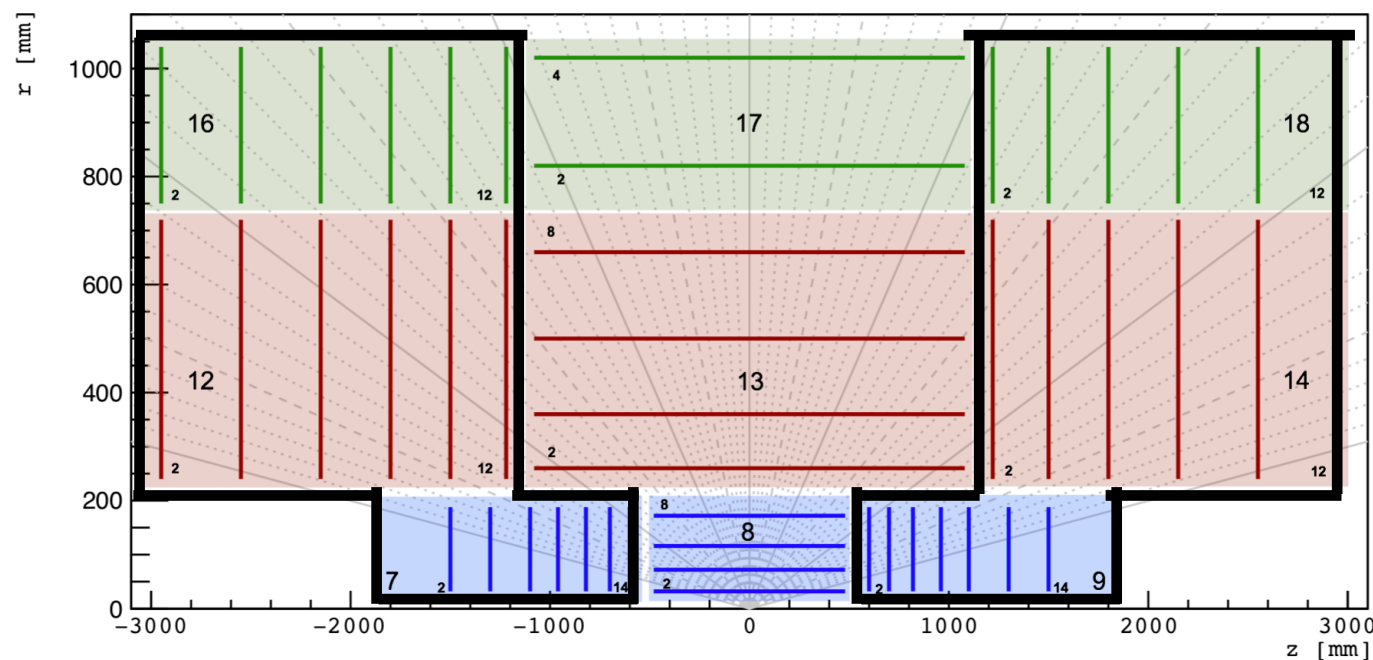


The data provides simulated hit positions in the inner detector with the geometry shown left, serving as a starting point, but not representing reality.



Latest layout of ATLAS Inner Tracker (ITk) [ATL-PHYS-PUB-2019-014](#)

Sophisticated layout in pixel endcap.



The data is to represent the HL-LHC conditions with  $\mu = 200$ .

One event has about 10k particles and 100k hits.

Out of the 10k particles, about 86% are **reconstructable**, defined as particles leaving hits in the detector

## Tackling the problem from a smaller dataset:

- Hits recorded in volume [8, 13, 17], basically barrel region
- Particles leaving fully connected tracks in the detector, i.e. no missing hits

# Track formation

Start with “Hits”

edge selection

Pairs

split into  $\eta$   $\phi$  regions

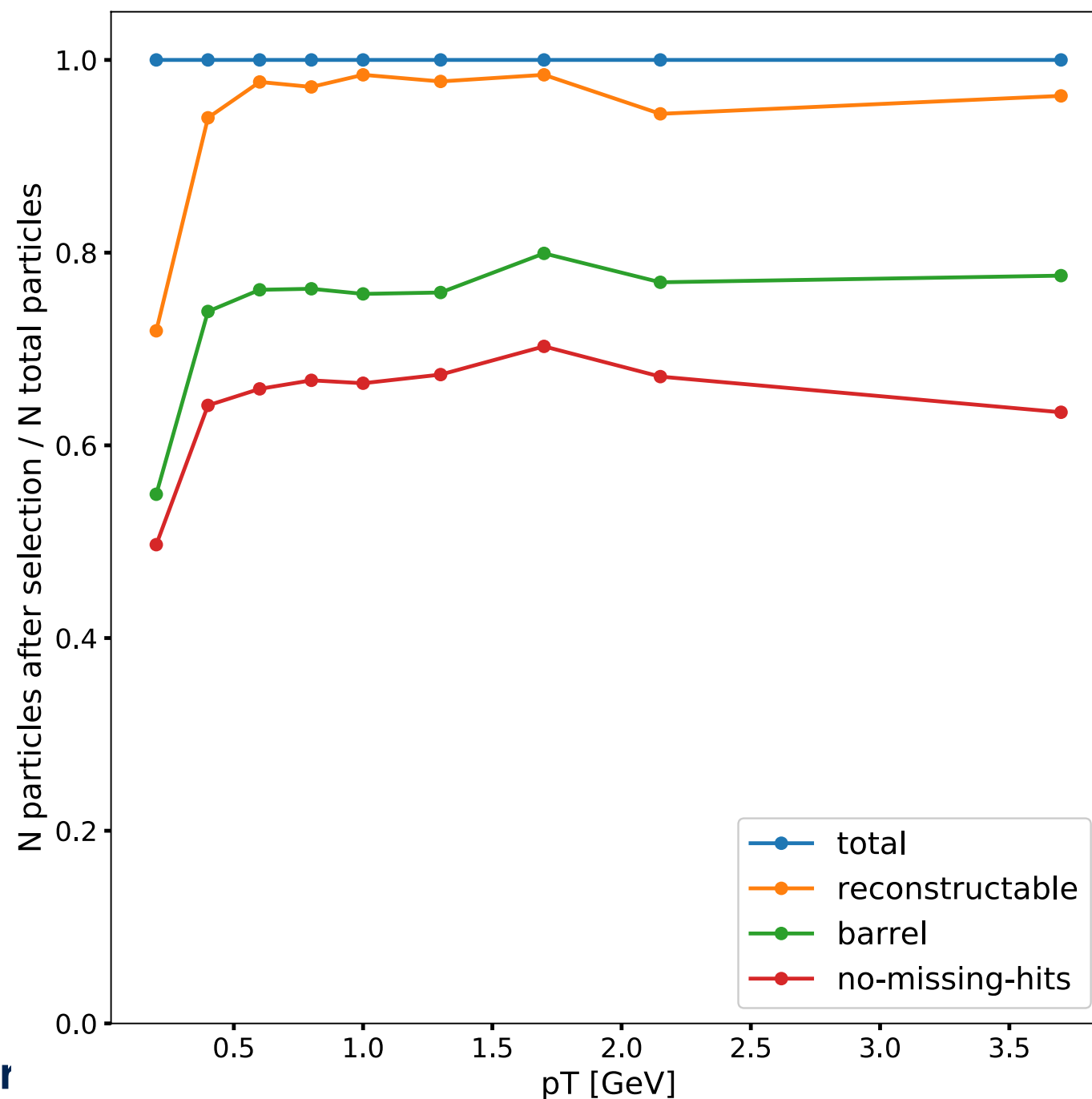
Graphs

GNN + CTD

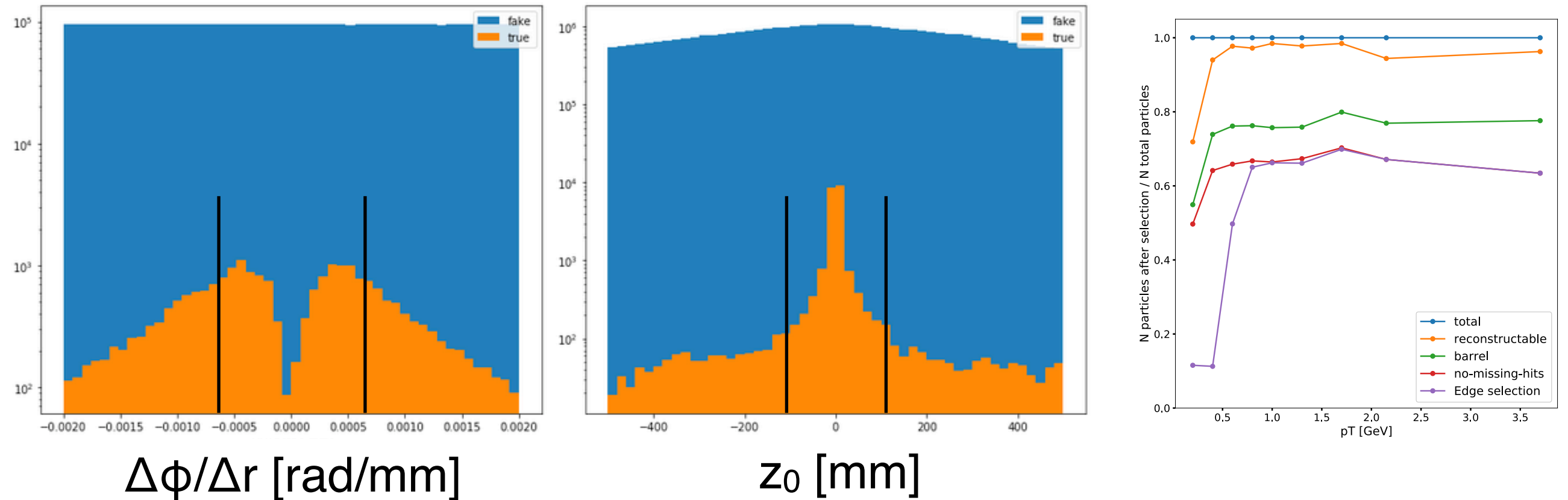
track candidates

Track candidates survive selections only when they have the exact hits as true tr

# of particles after stacked selections over the total # of particles in the event

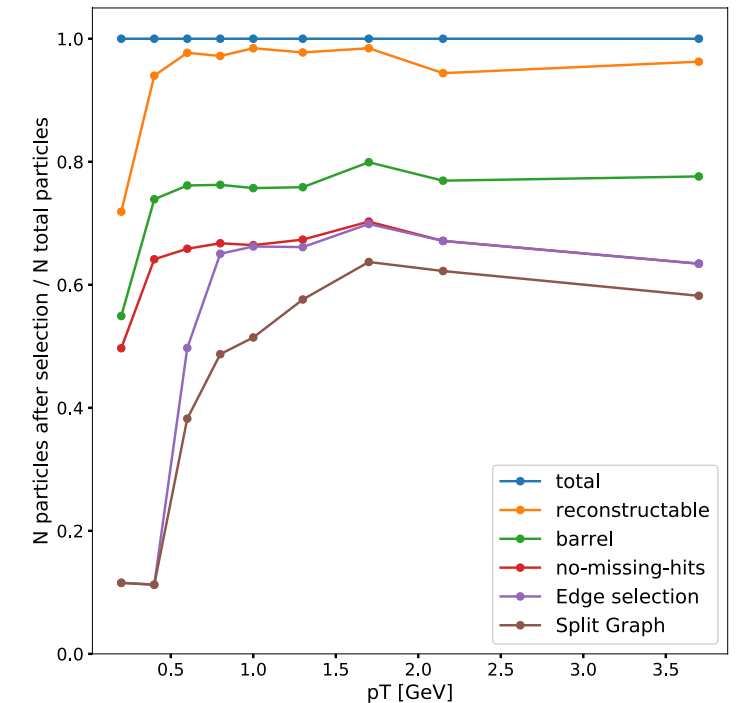
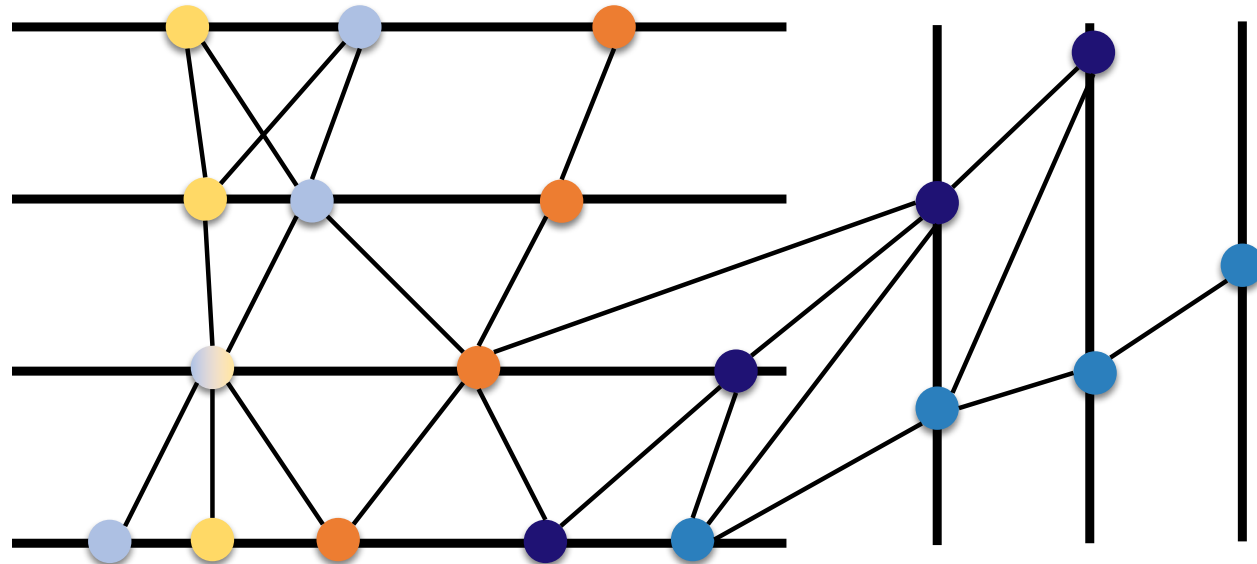


# Graph Formation: edge selection



- Make initial edges from hits in adjacent layers
- Use a simple selection to prune away fake edges
  - $\Delta\phi/\Delta r < 0.0006$ ,
  - $z_0$  (intercept of the line passing through the two hits)  $< 100$  mm
- Tuned to be efficient for tracks with  $p_T > 1$  GeV

# Graph Formation: construct graph from pairs

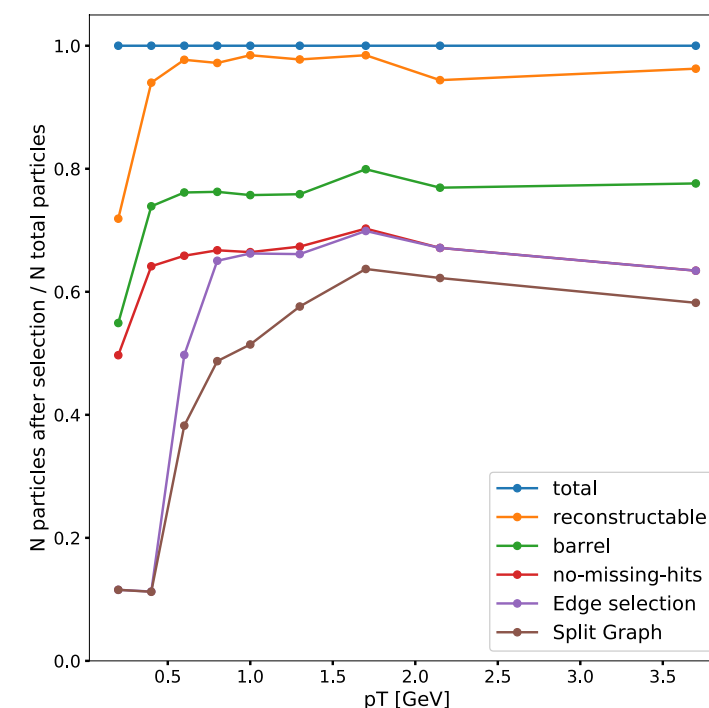
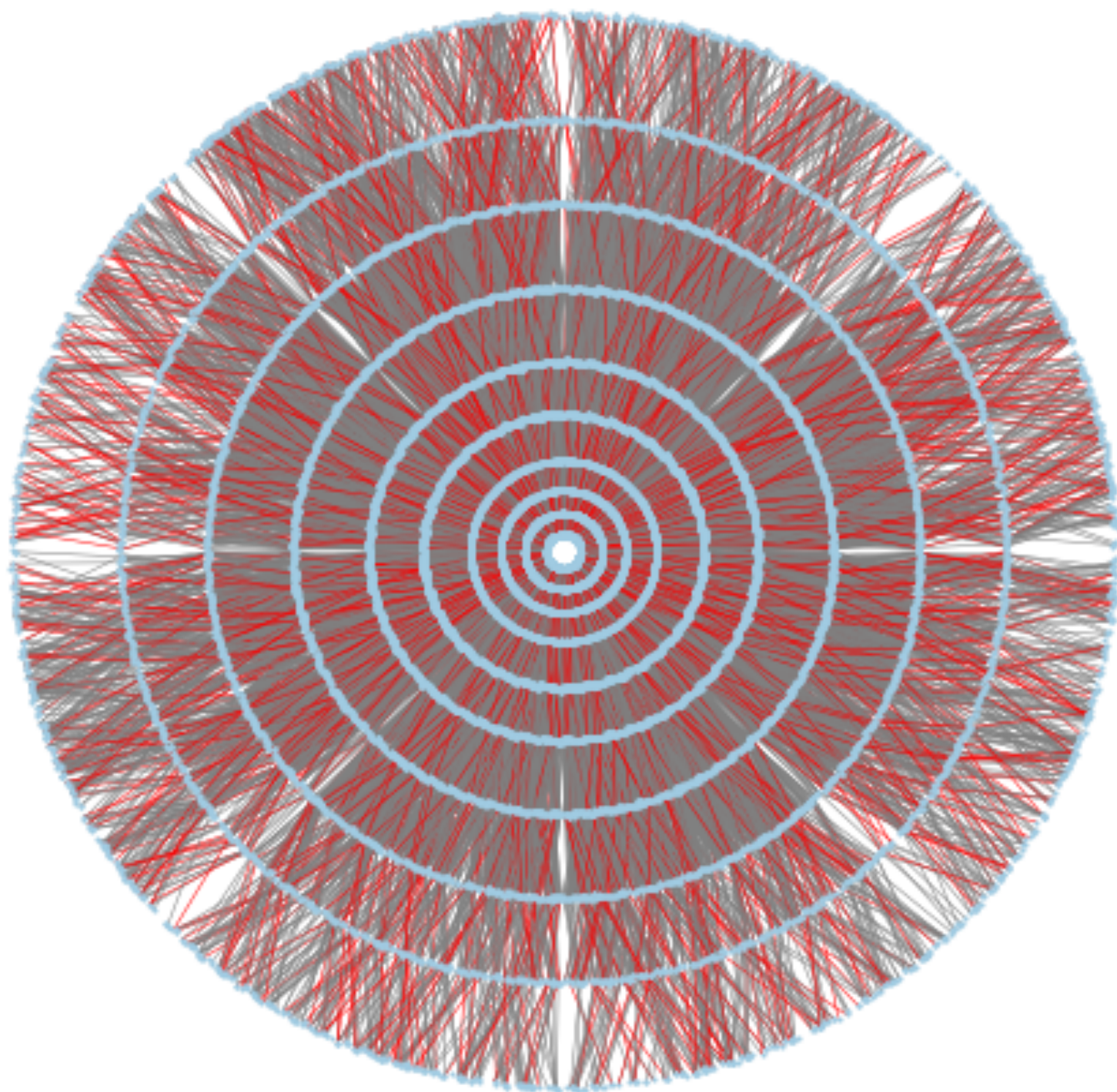


- Construct a directed graph, flowing inside-out
  - Split into 16 subgraphs, **8  $\phi$  bins and 2  $\eta$  bins**
    - need smart algorithm to deal with hits in boundaries
  - **input node features:**  $[r, \phi, z]$
  - Edges belong to a track assigned with score of 1, 0 otherwise



# Graph for one event

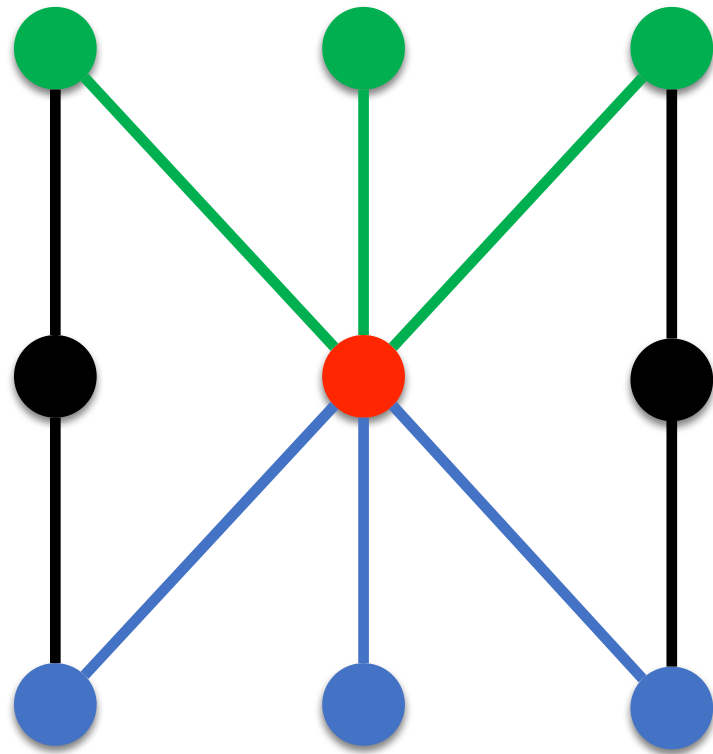
After all previous selections



- About 160k edges, 92% are fake (in gray)
- 8 gaps result from 8 sections in  $\phi$
- Can GNN find the 13k true edges out of the 147k fake ones?



# GNN Architecture



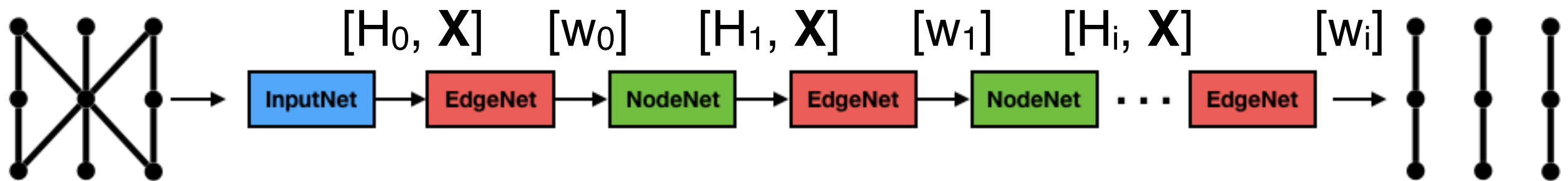
Three components operate on graph:

- **Input network** computes hidden node features
- **Edge network** computes **edge scores** from node features
- **Node network** computes hidden node features from aggregated **weighted incoming** and **outgoing** node features

Incoming and outgoing nodes with higher weights get more “attention”

# Putting them together

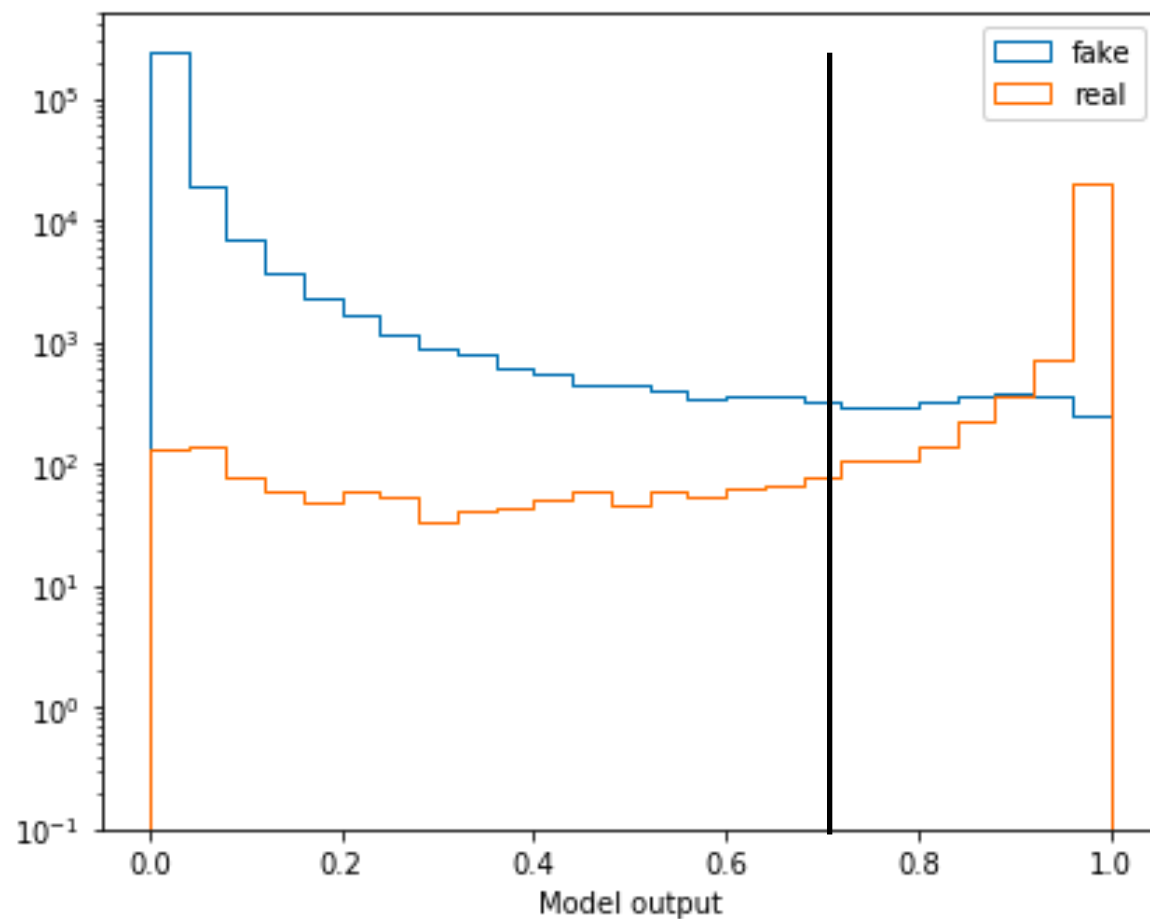
H: hidden states/features, X: input node features



- **EdgeNet and NodeNet iteratively applied 8 times, so 8 iterations**
- Message passed with the “attention mechanism”
- Hidden node features carry embedded track information for Edge Network to make predictions

# GNN Output and performance

- ~43k tunable parameters in pytorch
- Trained on [NVIDIA V100 'Volta' GPU](#) for about 60 epochs
- Weighted loss function



With a threshold of 0.7:

Edge Efficiency: 95.2%

Edge Purity: 90.2%

$$\text{Efficiency} = \frac{\# \text{ of True Edges passed the threshold}}{\# \text{ of total True Edges}}$$

$$\text{Purity} = \frac{\# \text{ of True Edges passed the threshold}}{\# \text{ of total Edges passed the threshold}}$$

- One can use higher threshold to gain purity at the cost of less efficiency.

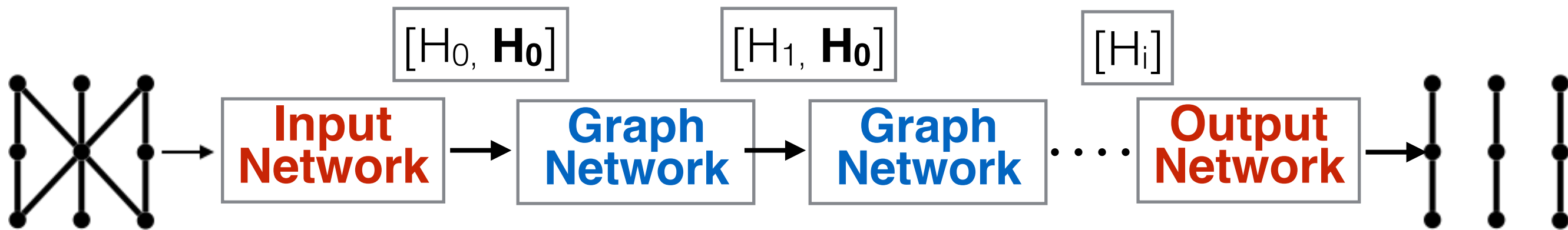
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*We are exploring other GNN architectures to push the performance further.*

*Following example uses graph\_nets library from DeepMind and a model resembling the Interaction Networks [[link](#)]*



# Alternative implementation of GNN

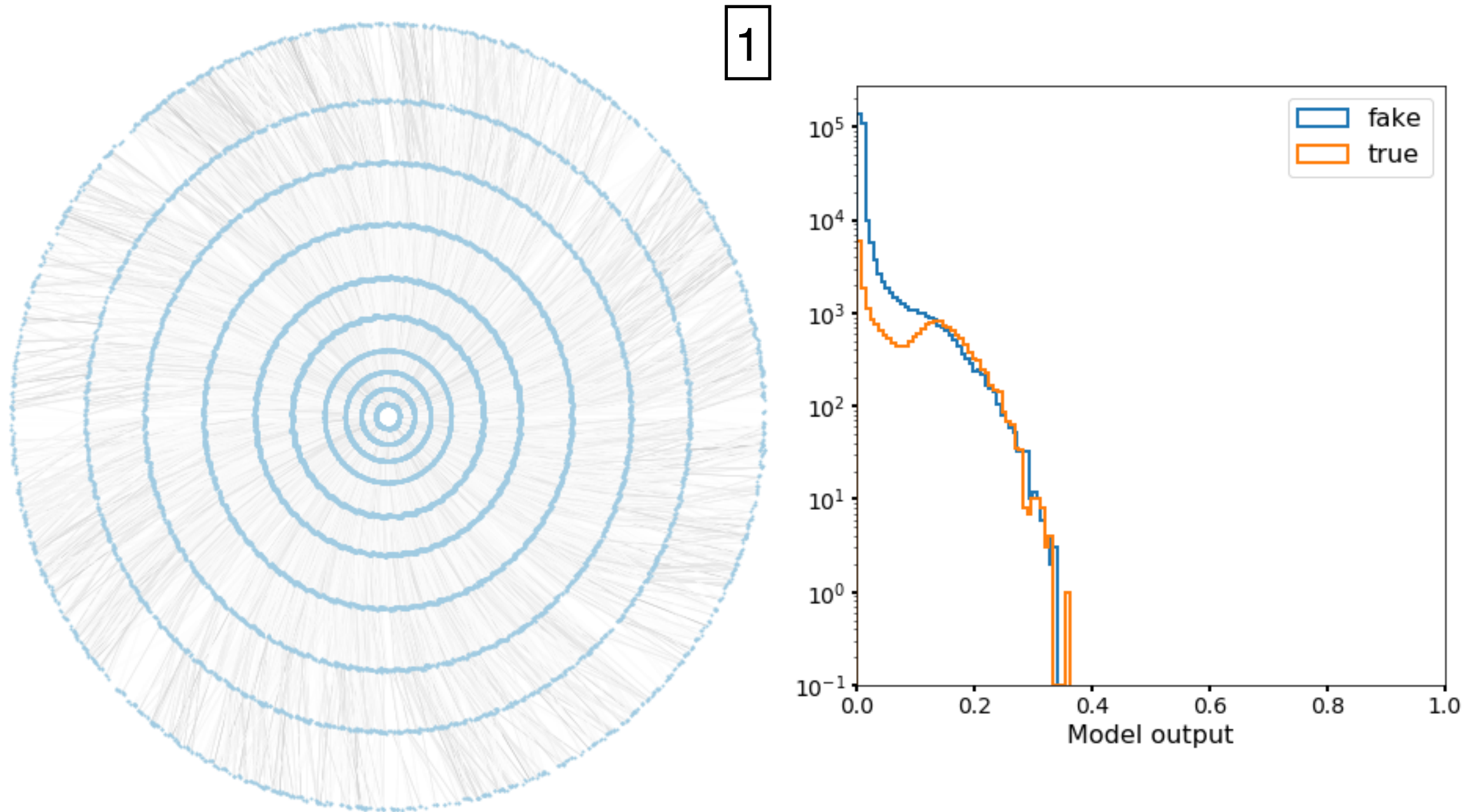


Differences:

- Edge features provided in the input
- Alternate message passing implementation:
  - No explicit attention mechanism
  - Edge features are computed from node features and then summed across all neighbors
- Output Network computes final edge scores
- Bigger, deeper model (266k parameters)

We can visualize the intermediate outputs of the model

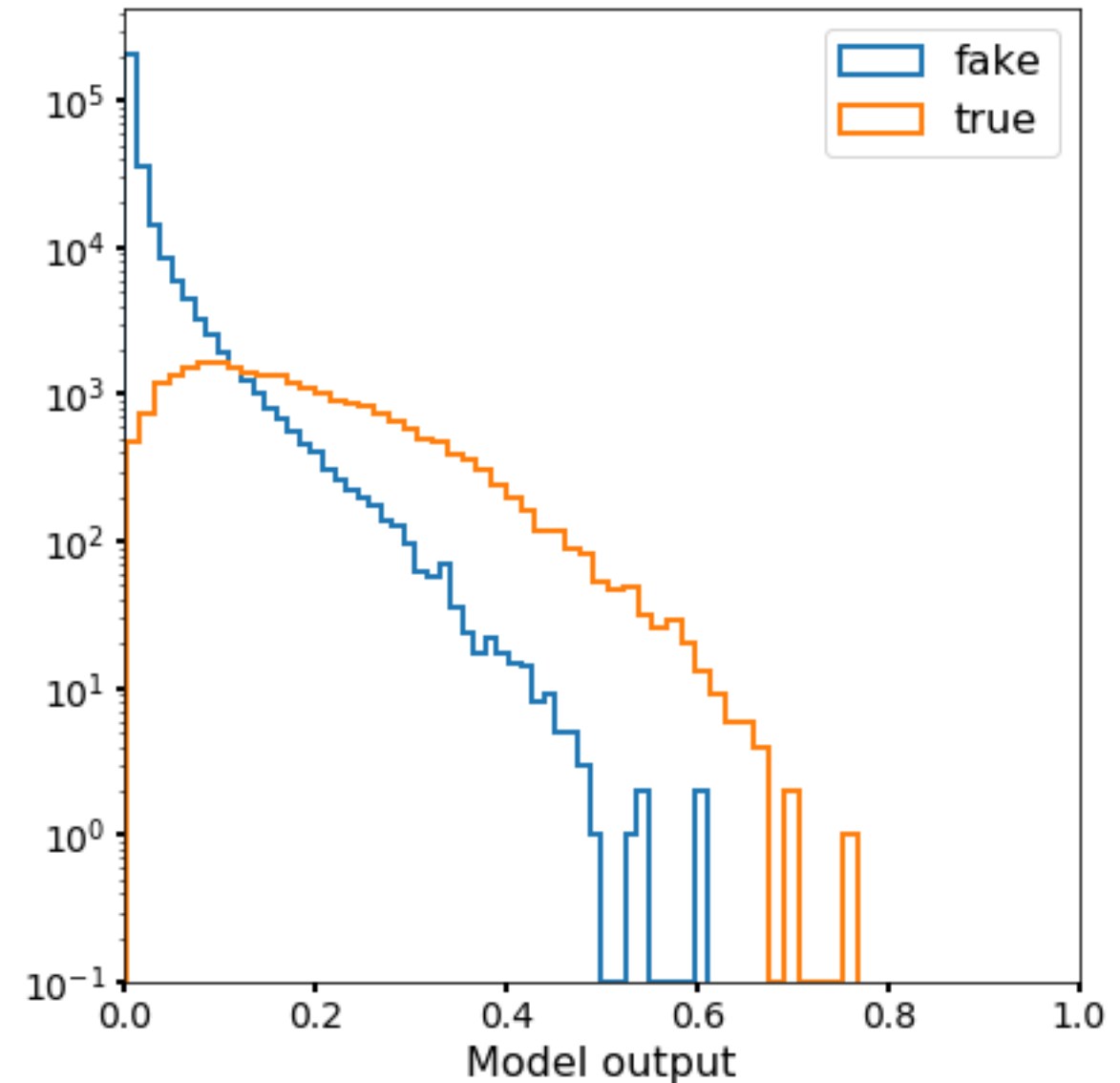
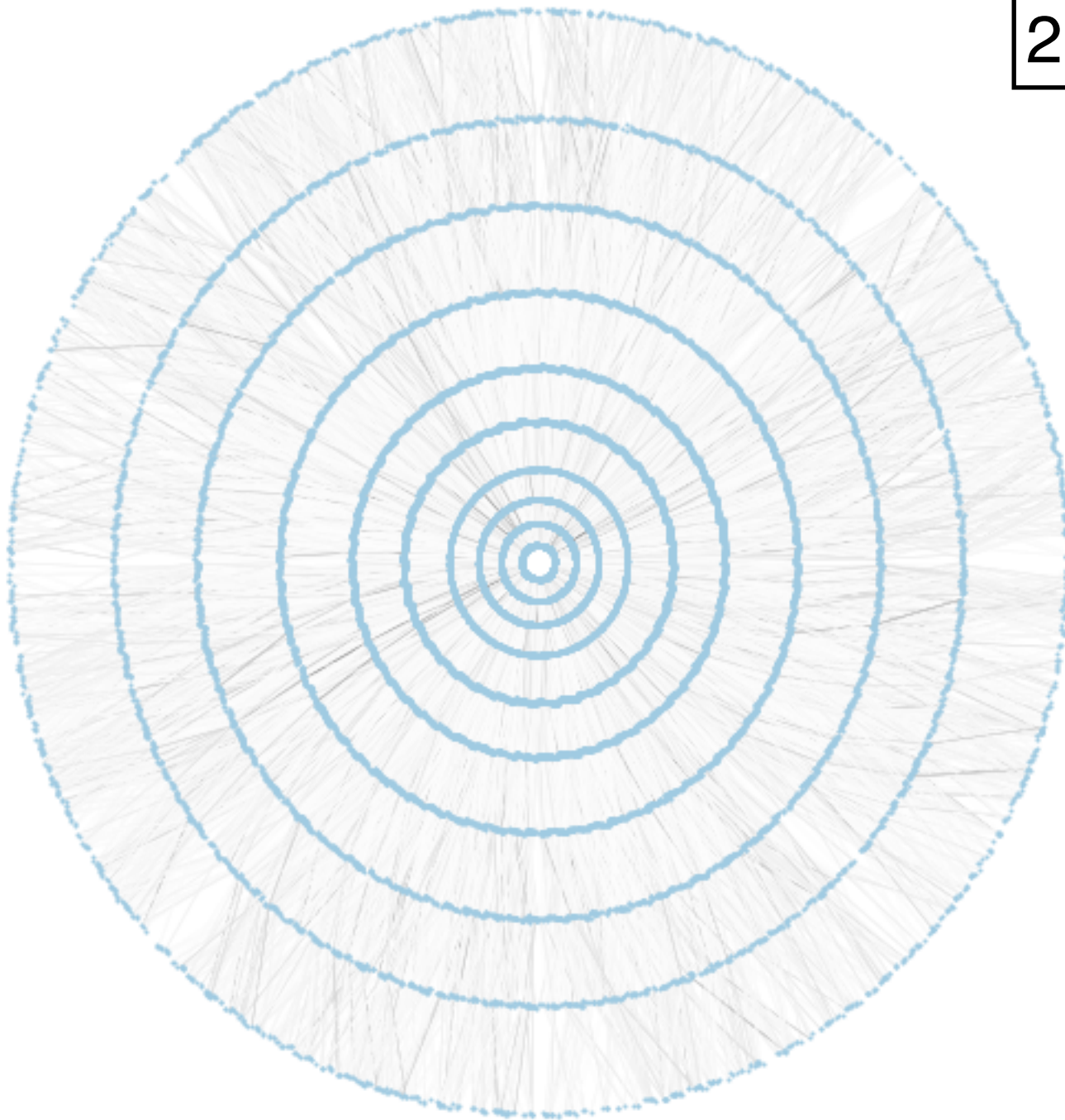
# Predicted score improves after each iteration



Edges with higher scores are darker than that with lower scores  
Edges with scores  $< 0.01$  are removed for visualization purpose.

# Predicted score improves after each iteration

2

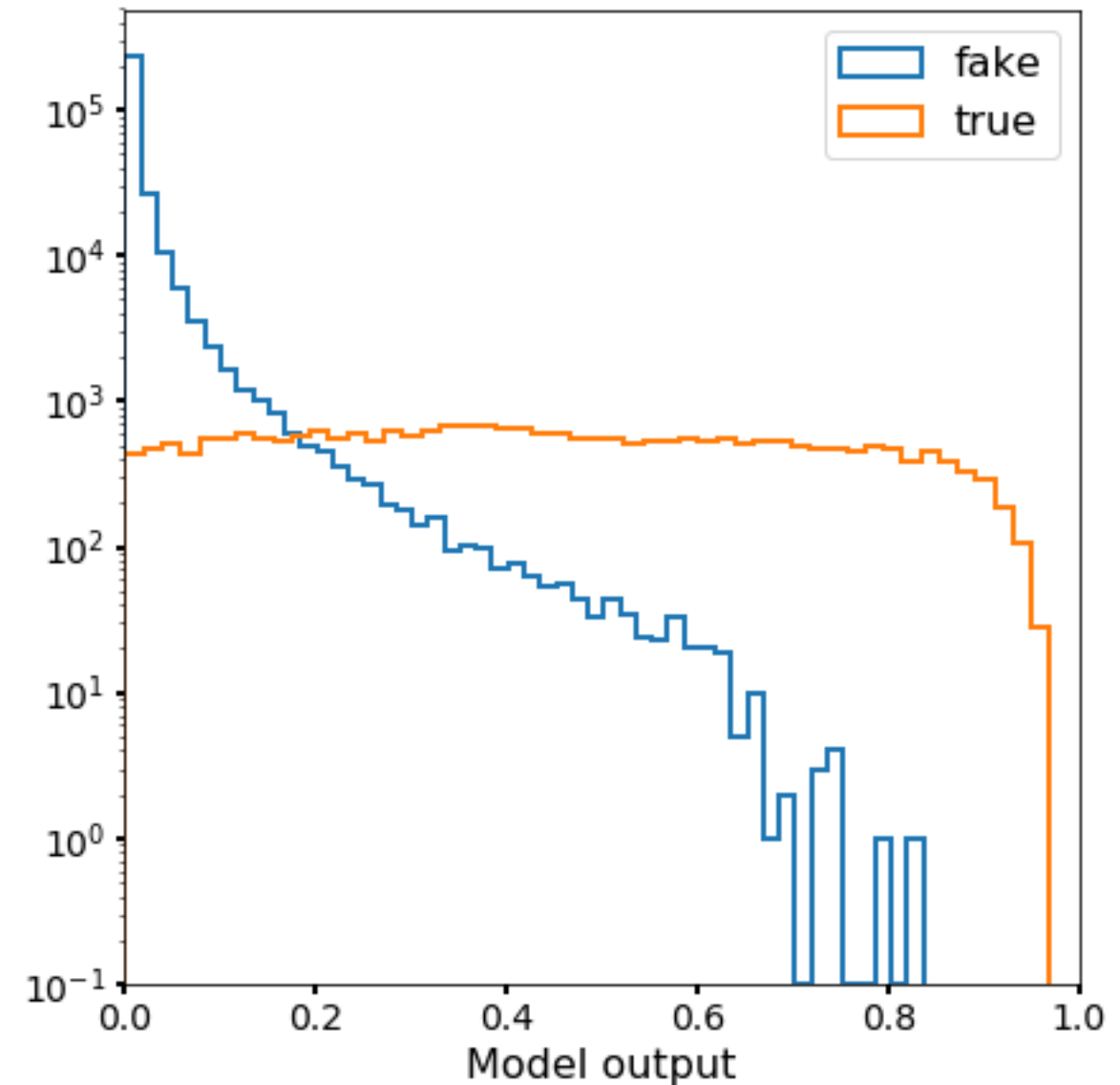
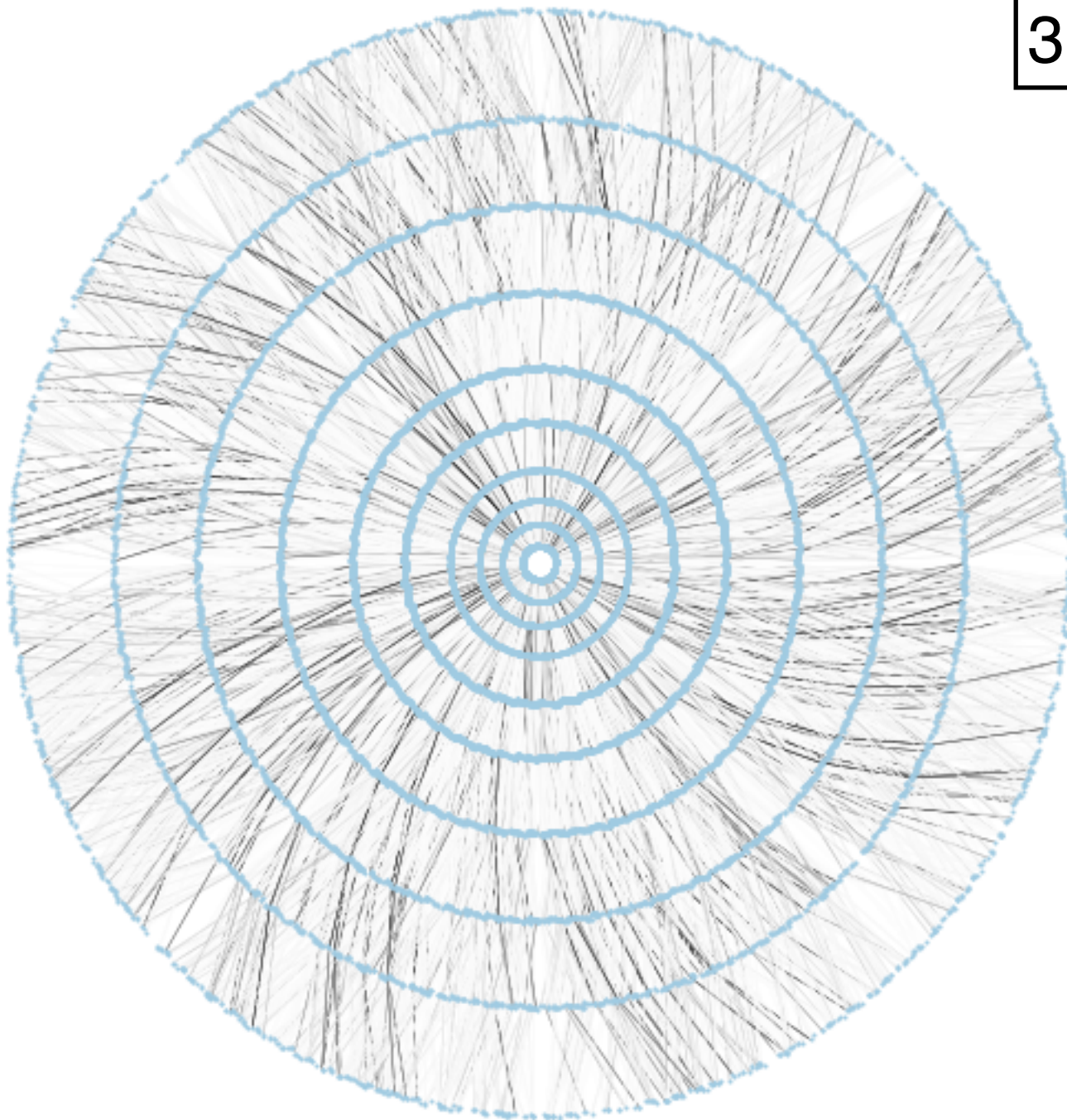


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# Predicted score improves after each iteration

3

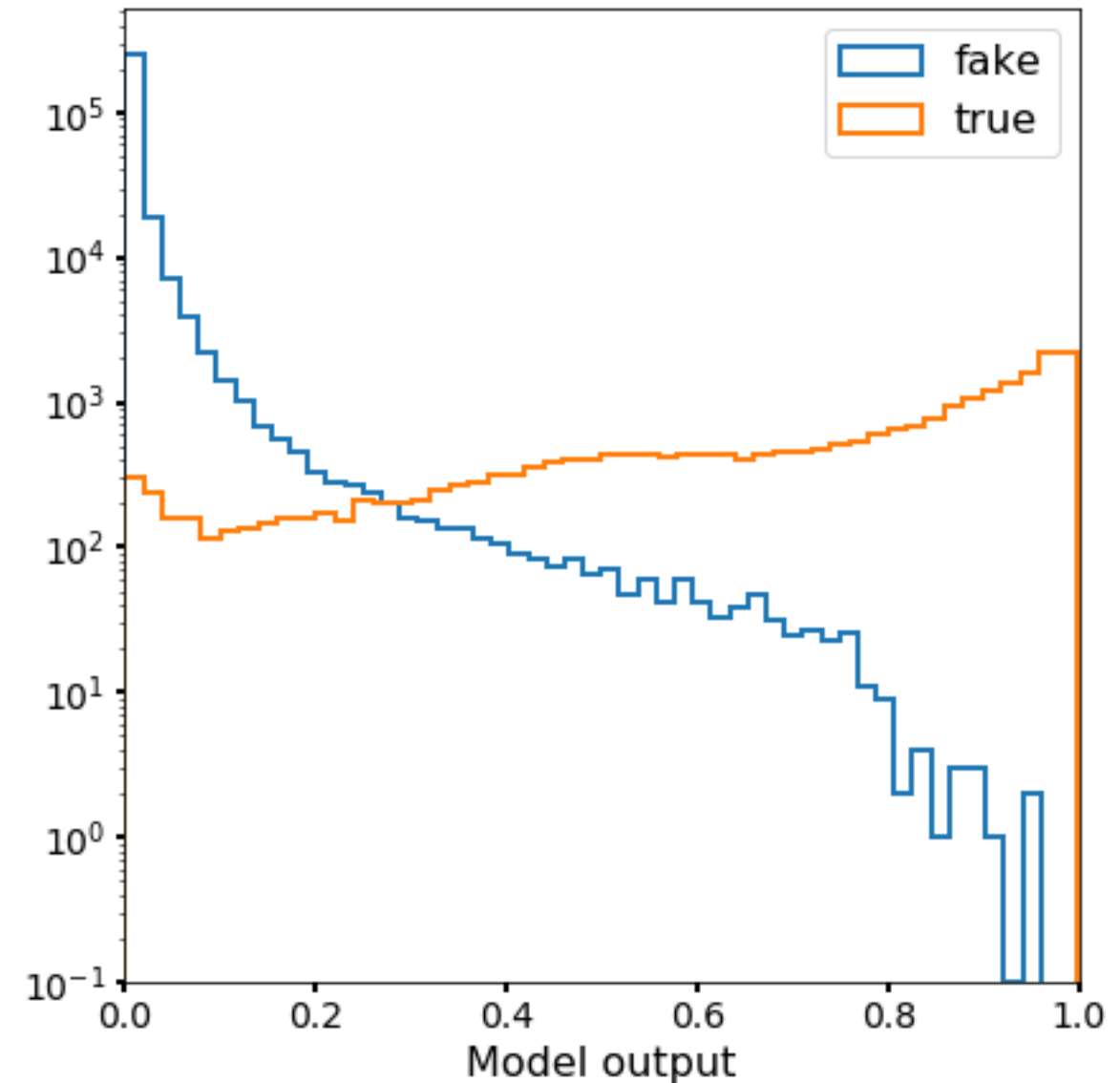
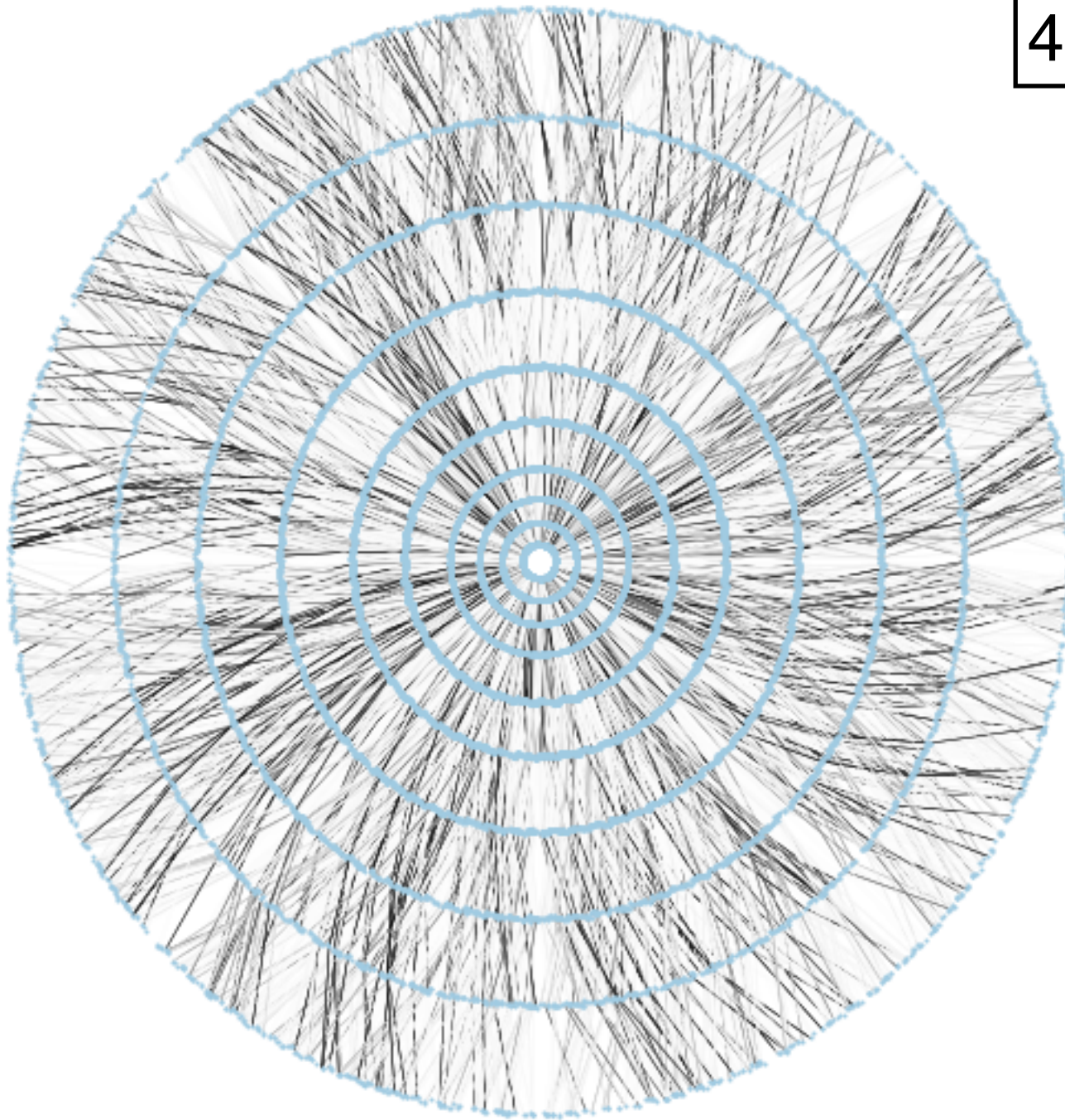


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# Predicted score improves after each iteration

4

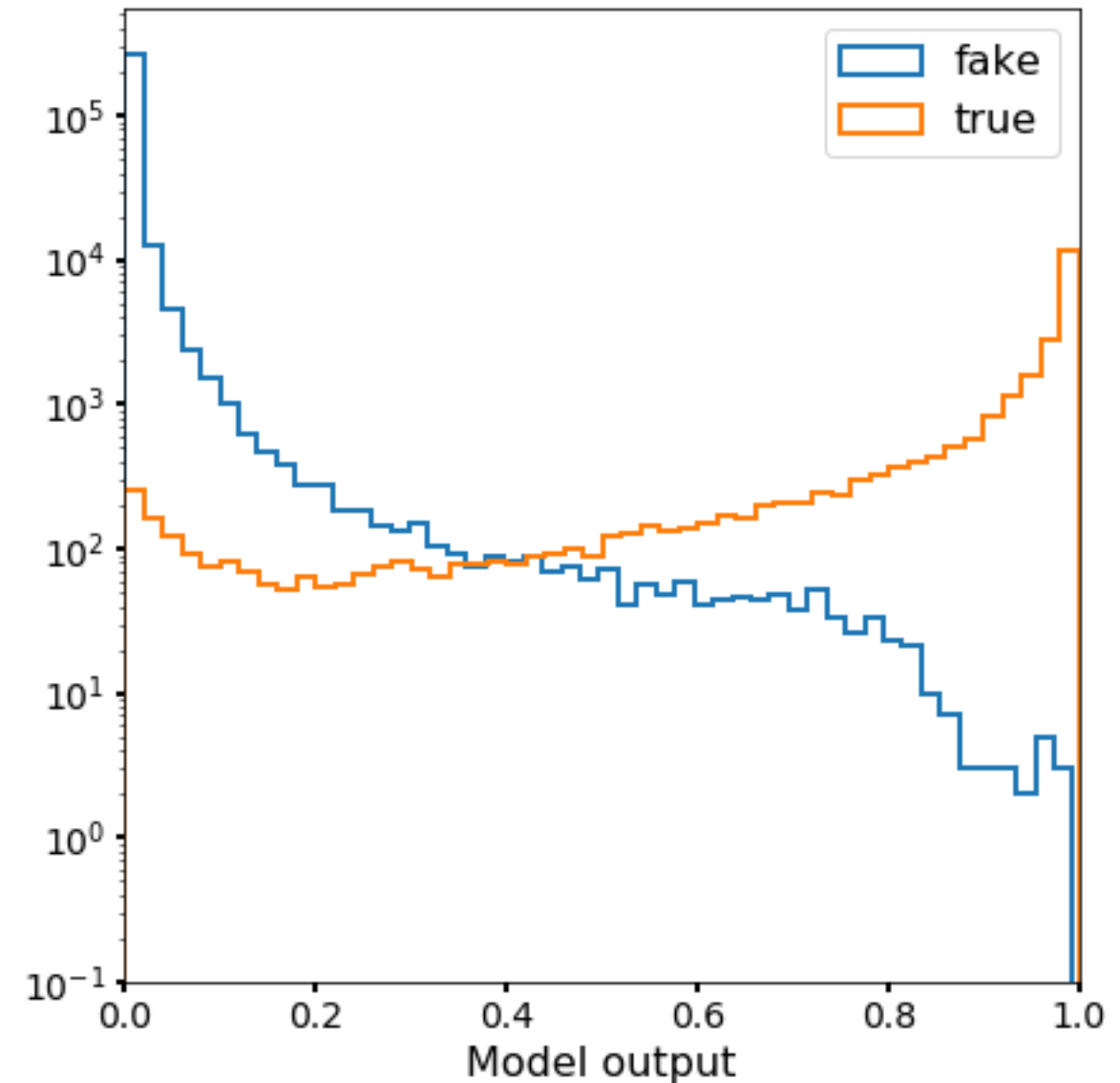
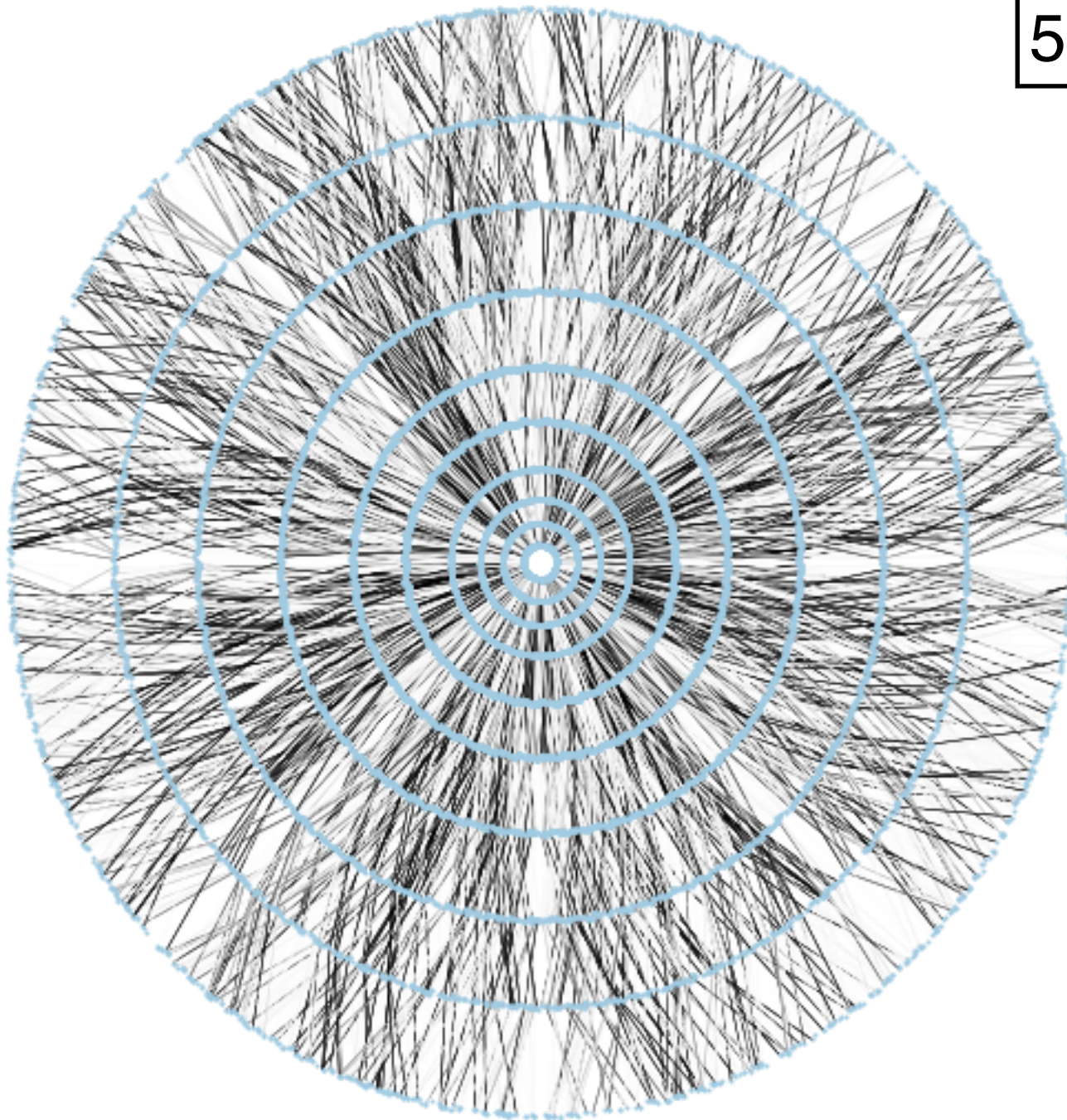


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# Predicted score improves after each iteration

5

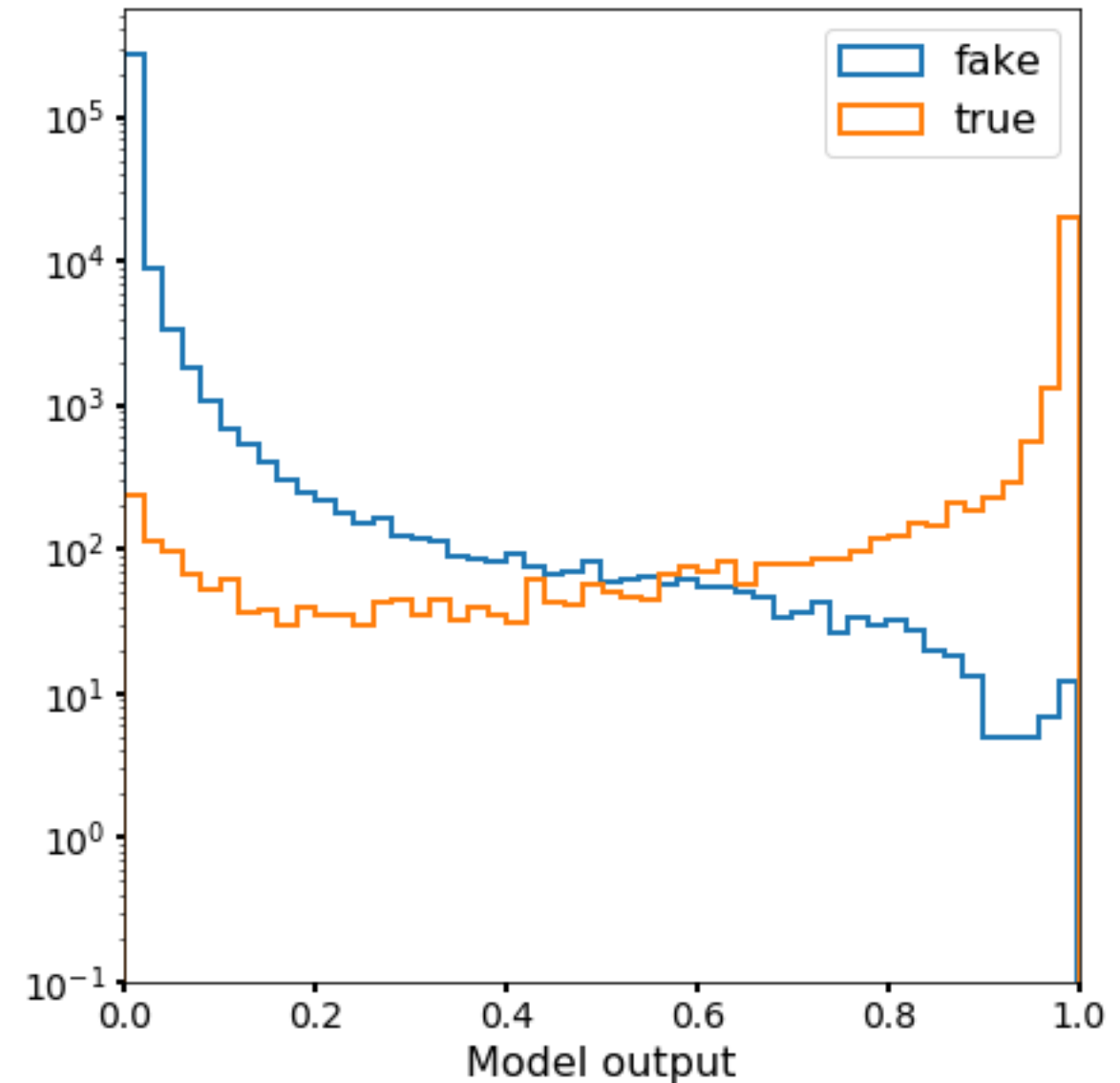
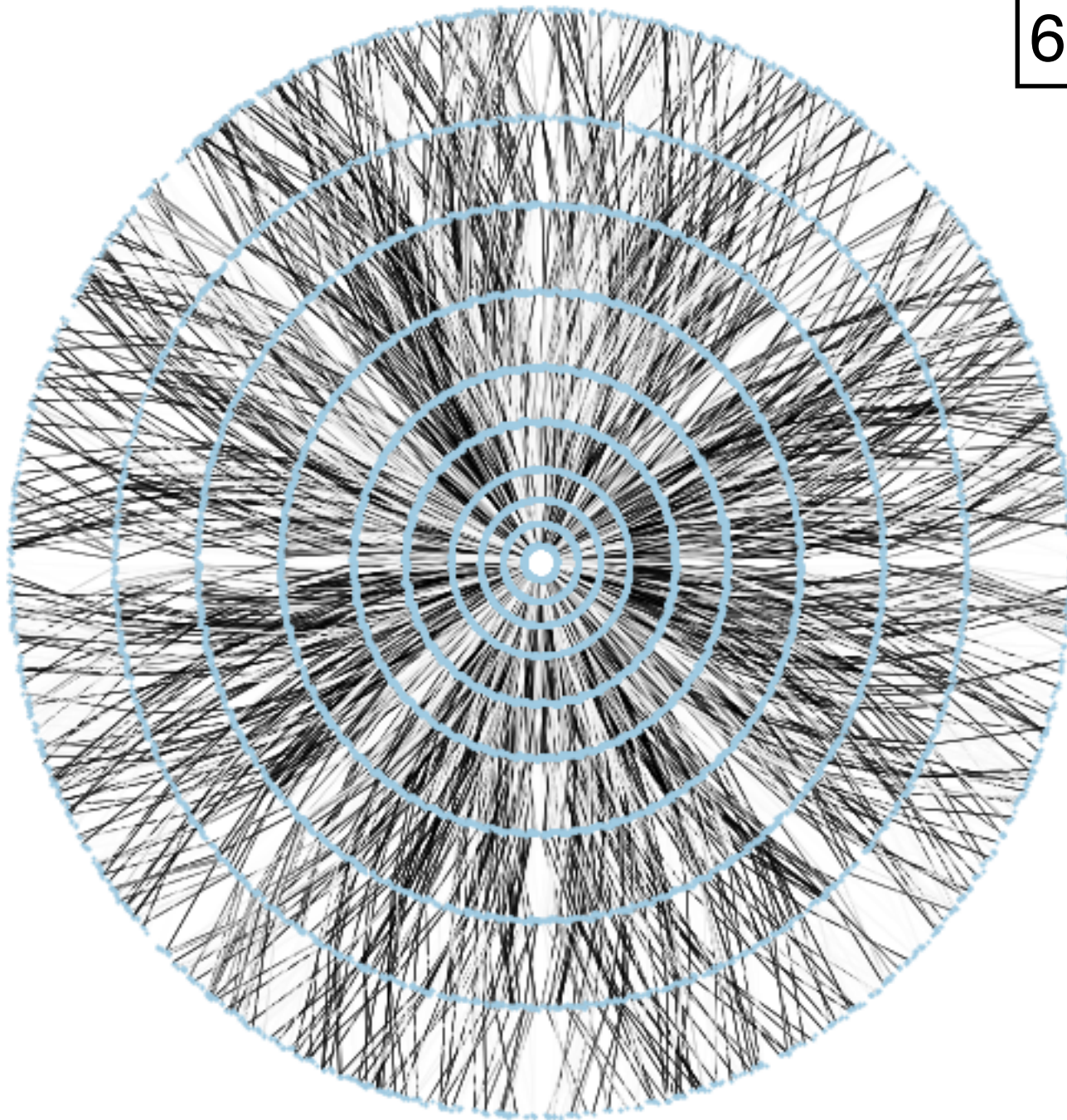


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# Predicted score improves after each iteration

6

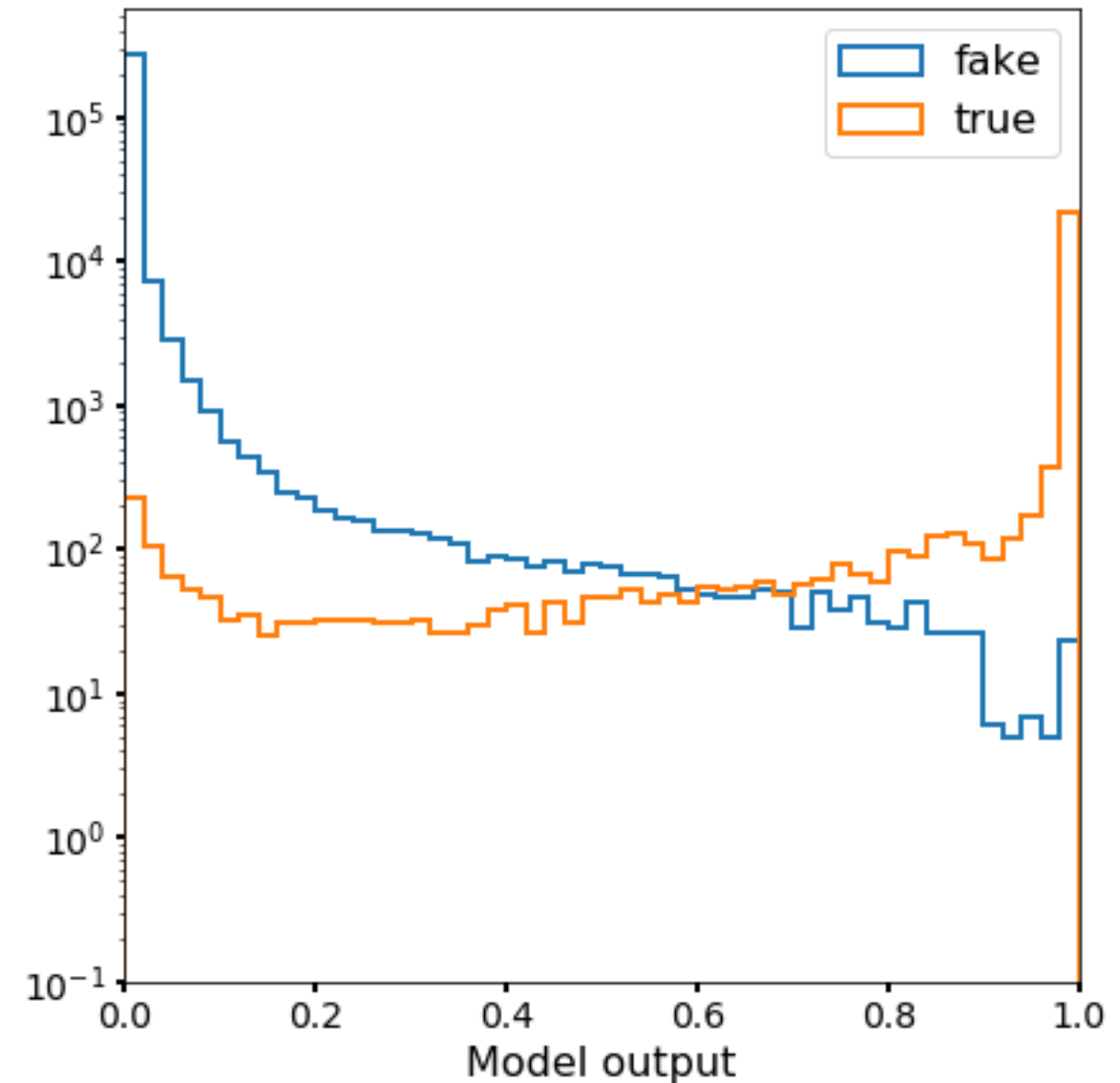
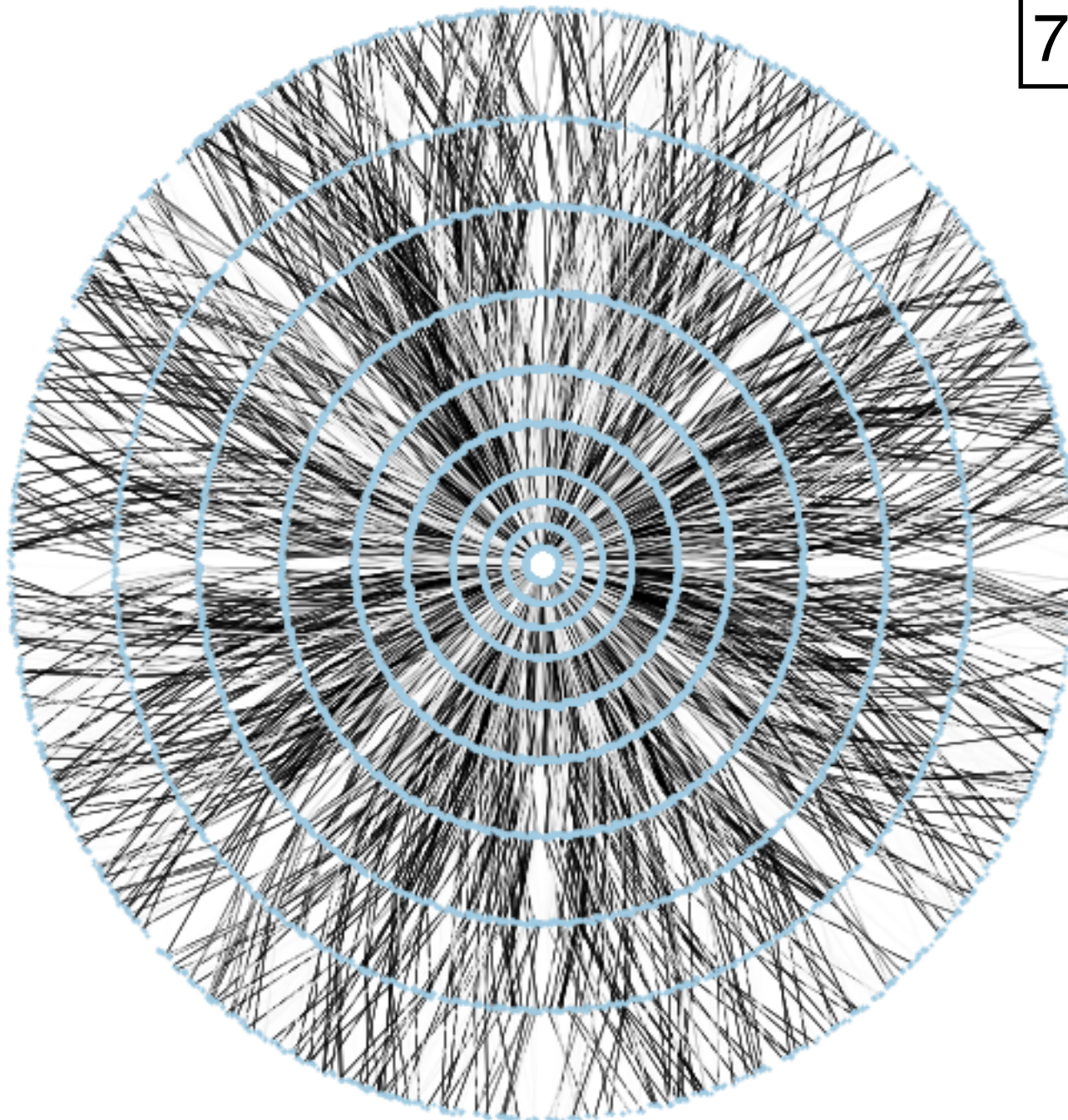


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# Predicted score improves after each iteration

7

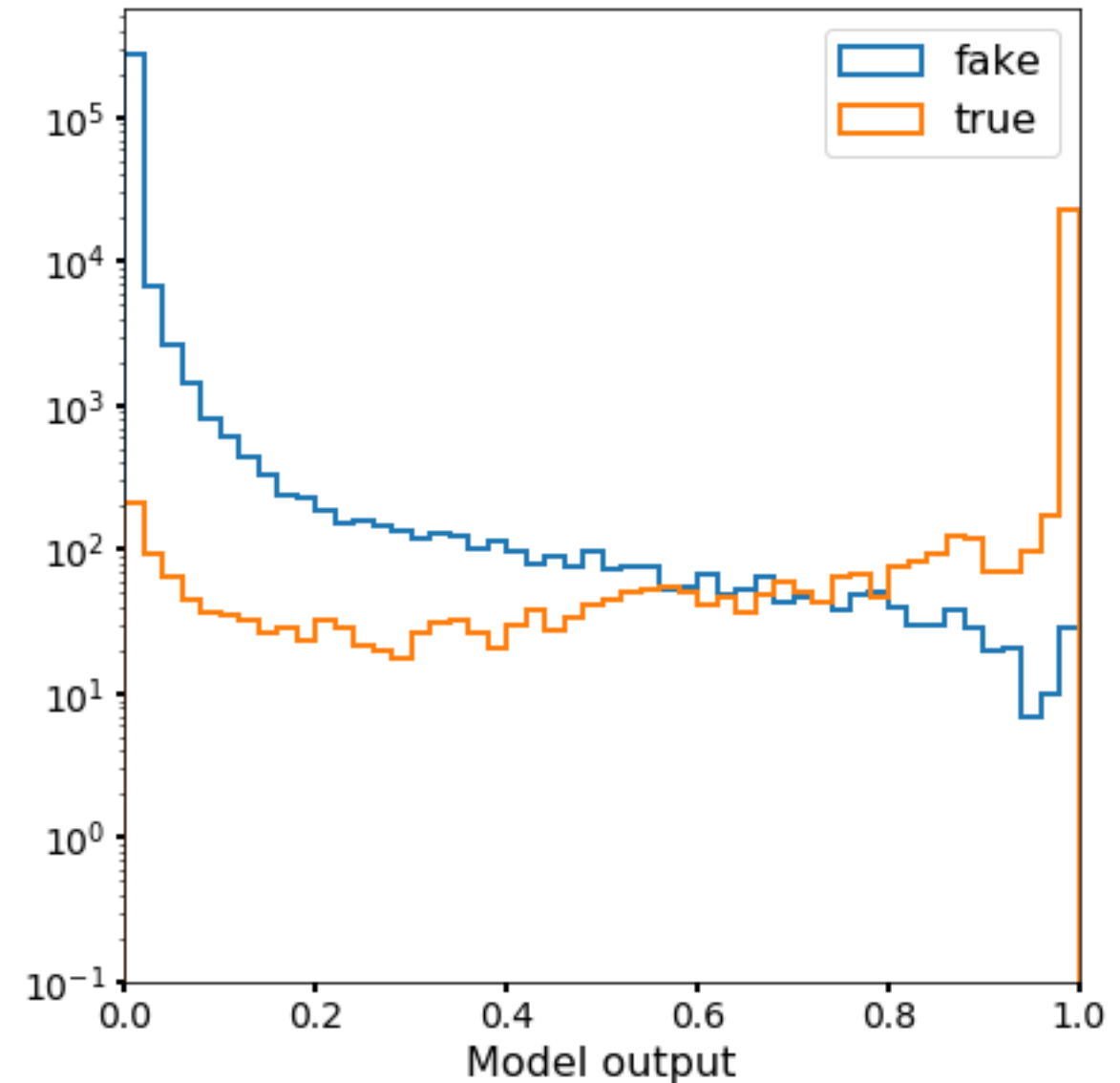
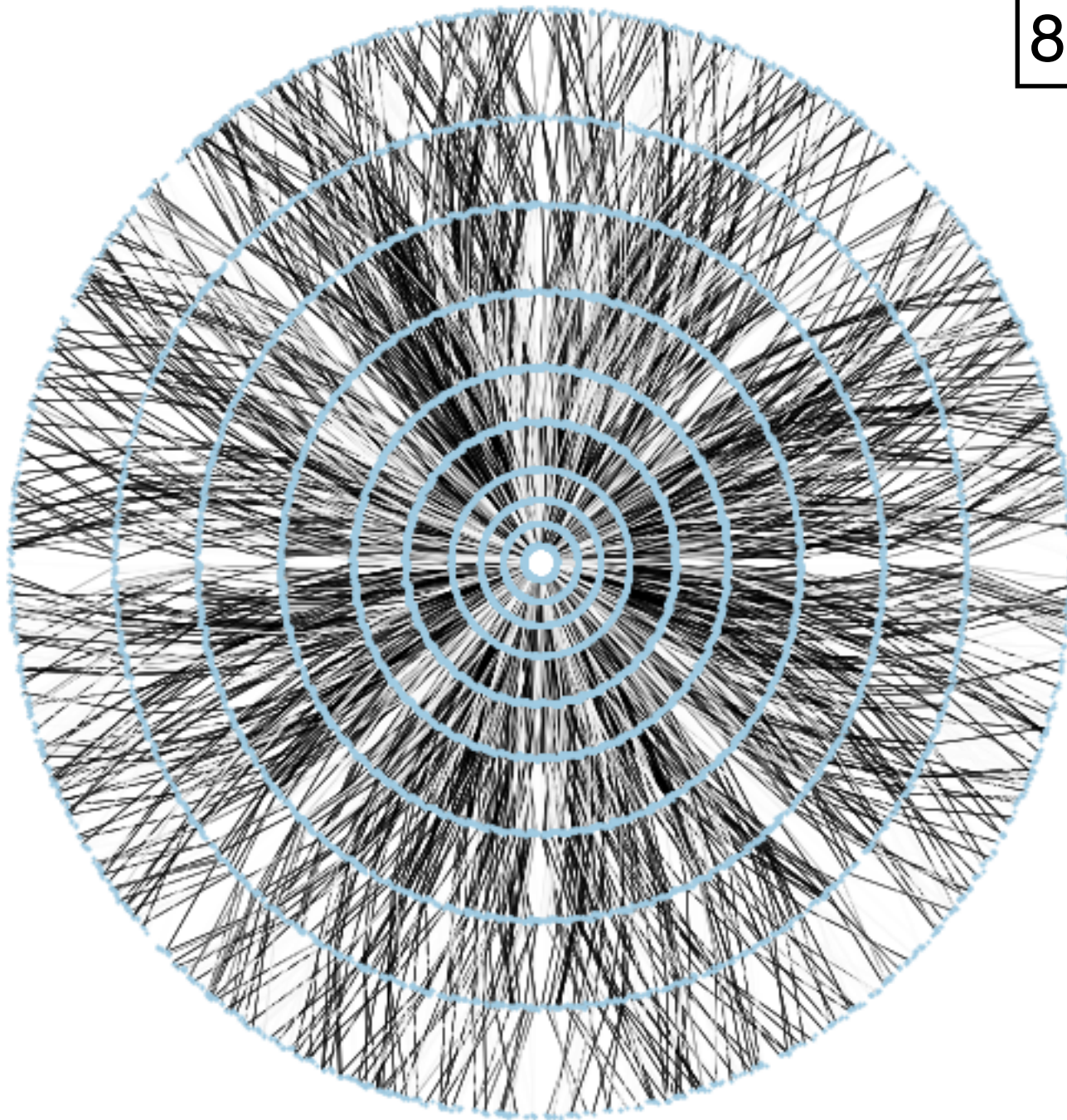


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# Predicted score improves after each iteration

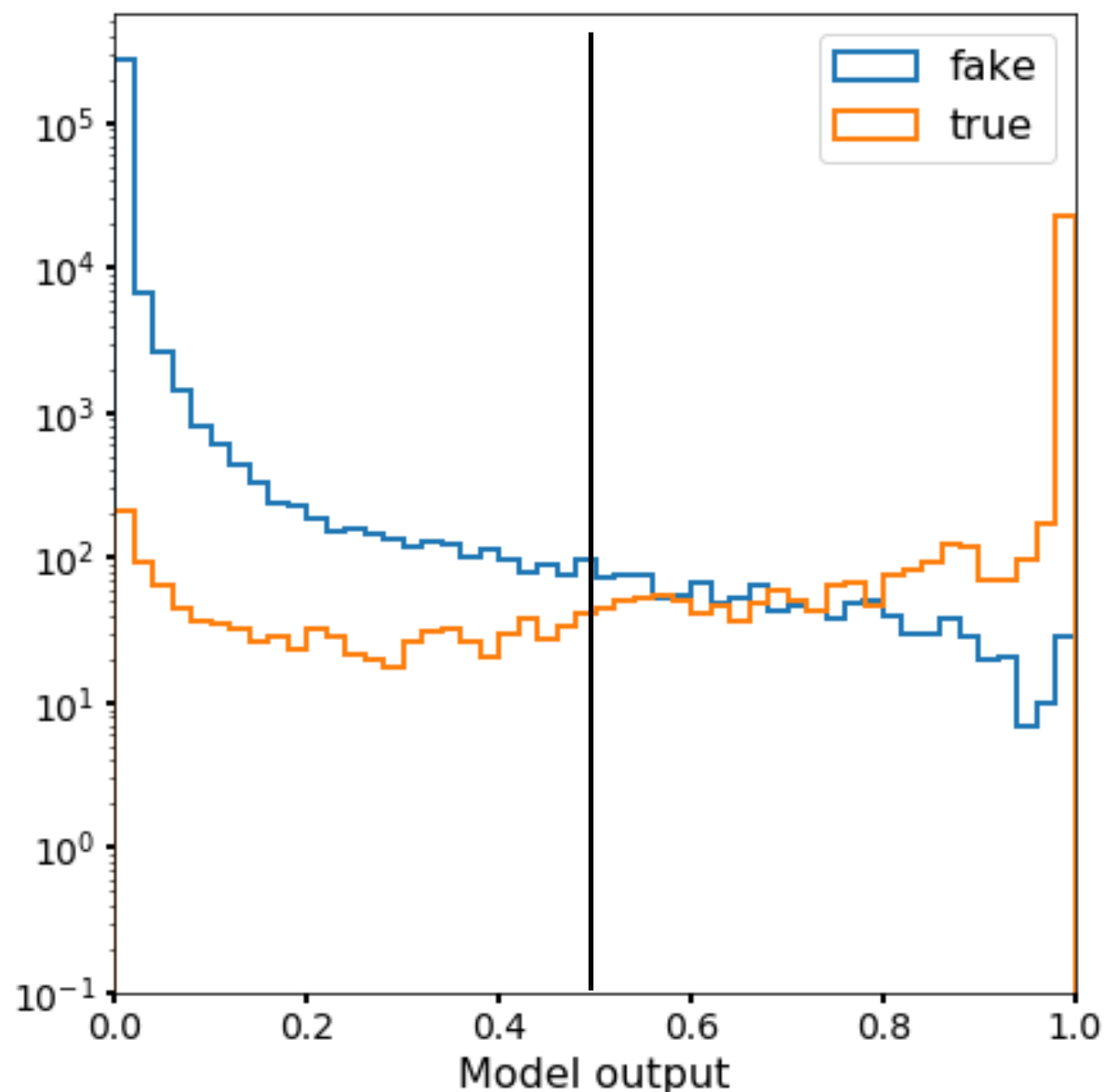
8



Edges with higher scores are darker than that with lower scores  
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# Performances

- ~266k tunable parameters in TensorFlow
- Trained on a GPU for about 2 epochs
- Weighted loss function

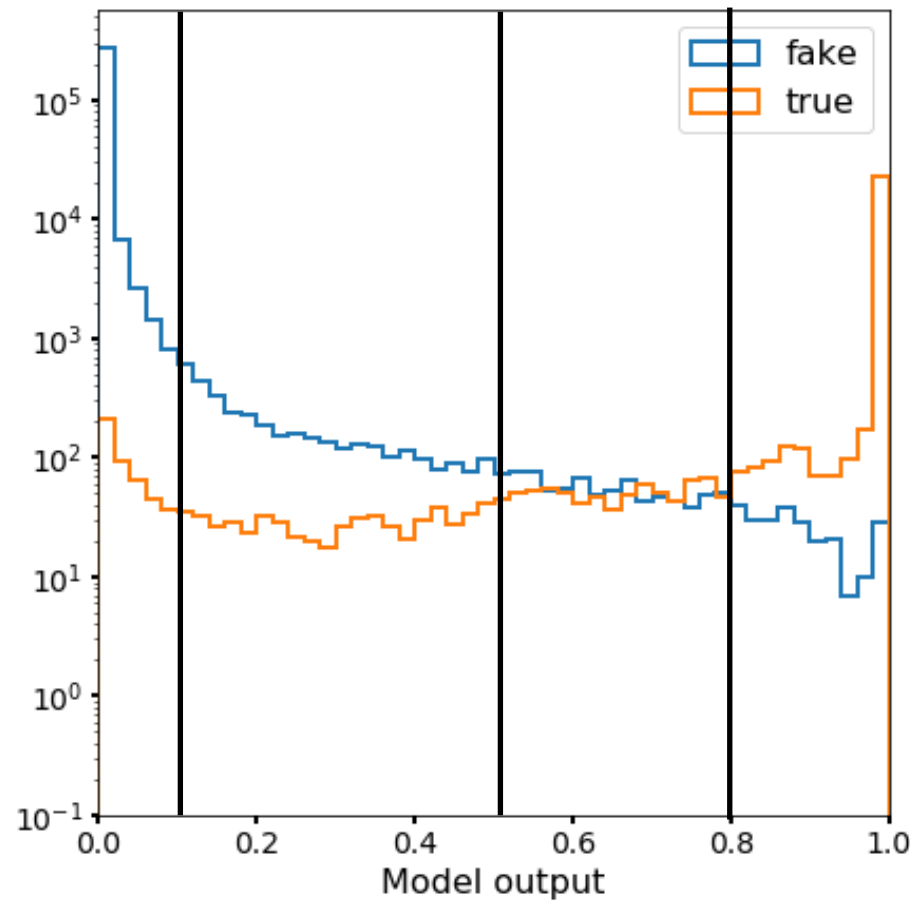


Threshold	0.1	0.5	0.8
Edge Efficiency	98.2%	95.9%	93.0%
Edge Purity	84.0%	95.7%	98.9%

$$\text{Efficiency} = \frac{\# \text{ of True Edges passed the threshold}}{\# \text{ of total True Edges}}$$

$$\text{Purity} = \frac{\# \text{ of True Edges passed the threshold}}{\# \text{ of total Edges passed the threshold}}$$

# Connect The Dots, a simple algorithm



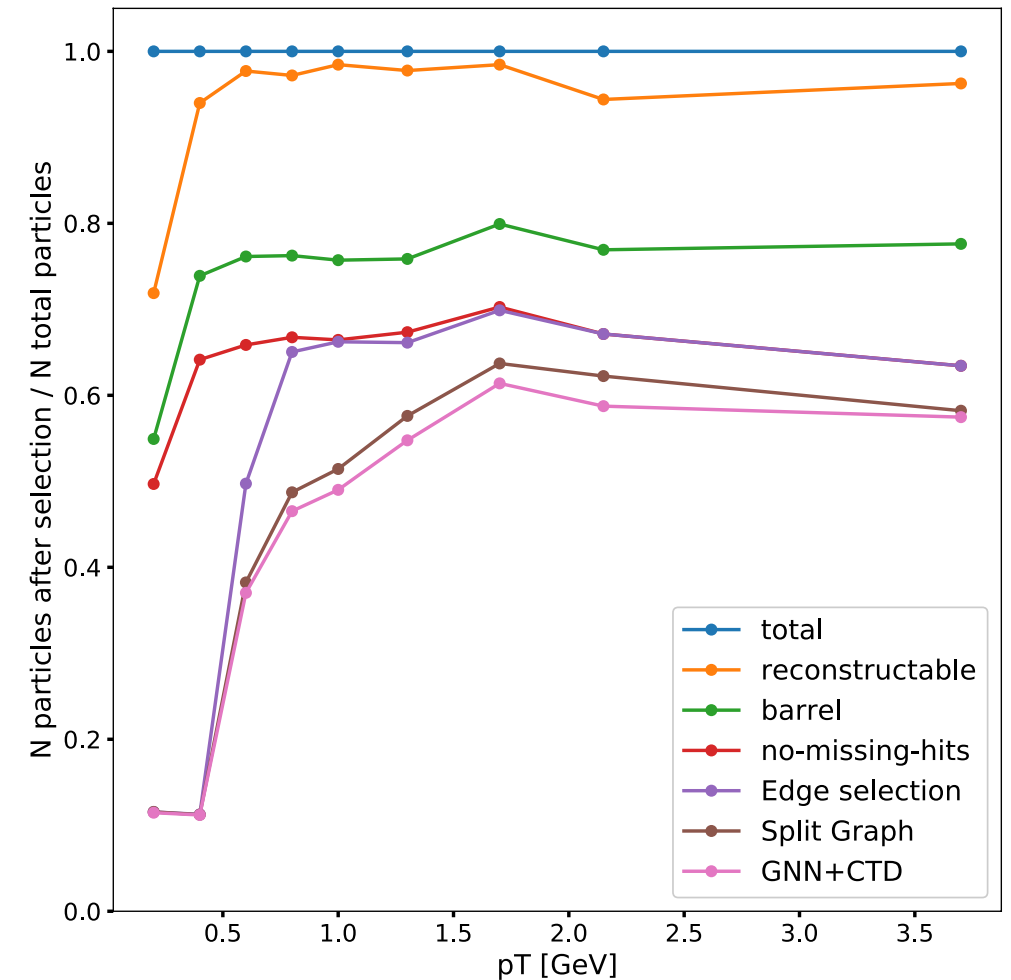
**Guided by edge scores from GNN**, we walk through the graph from inside to outside along edges with the maximum score that is **> 0.1**, as ones  $< 0.1$  having high probability being fake

Add paths with scores **> 0.8** → having high probability being true

- Longest path is selected for the starting hit, then go to next not-used hit.
- Each hit is assigned to one track.
  - We will lift the constraint to gain efficiency and robustness, and then resolve ambiguities.

# A summary

one-event	N-particles	ratio w.r.t Total	ratio w.r.t Reconstructable	relative ratio
Total	11170	100%		100%
Reconstructable	9635	86%	100%	86%
Barrel	7492	67%	78%	78%
No-missing hits	6600	59%	69%	88%
Edge selection	3114	28%	32%	<b>47%</b>
Split graph	2668	24%	28%	<b>86%</b>
GNN	2590	23%	27%	<b>97%</b>

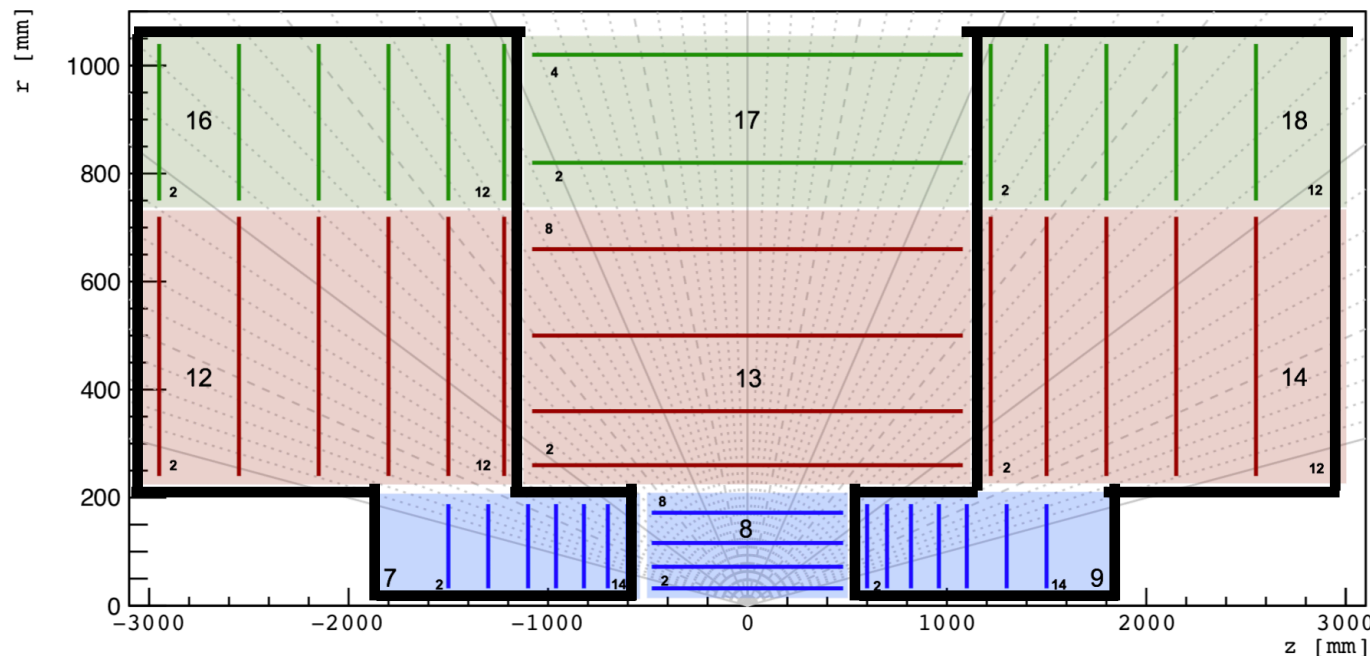


GNN edge classifier achieves over 95% efficiency across the pT range with a purity greater than 95%



# Edge selections

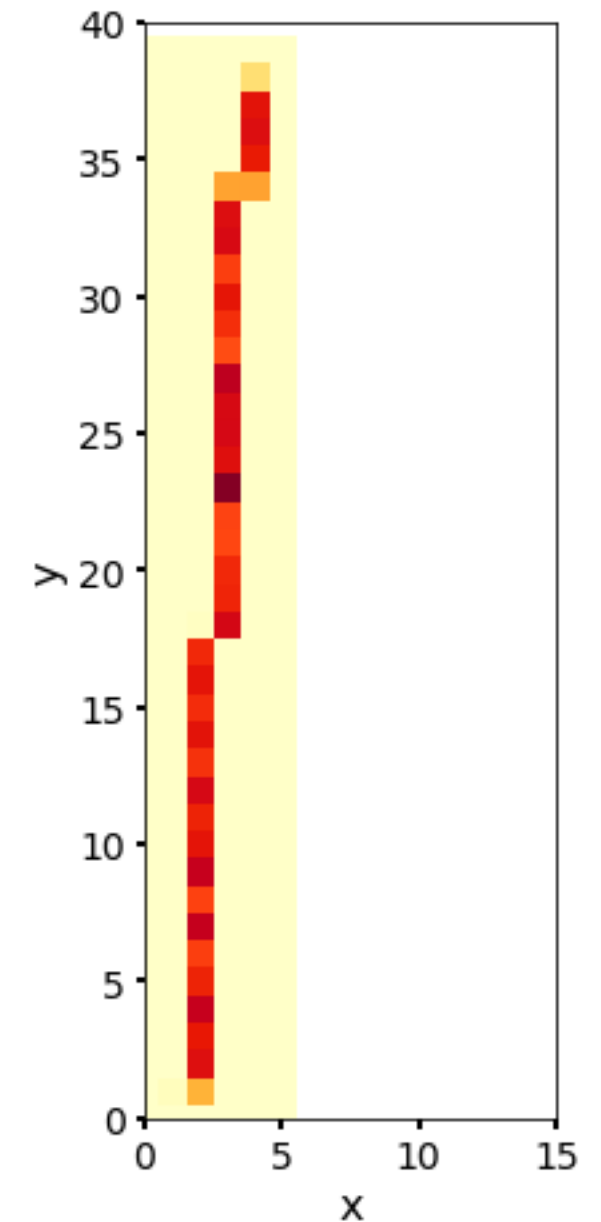
- Current selections tuned to be efficiency for tracks with  $p_T > 1$  GeV in barrel.
  - Not tested in endcap (probability need tuning)
- Explore simple neural networks to do the job:
  - No need of engineering variables
  - Applicable to all hits pairing (barrel and endcap)
  - Can easily use GPU and be parallelized.



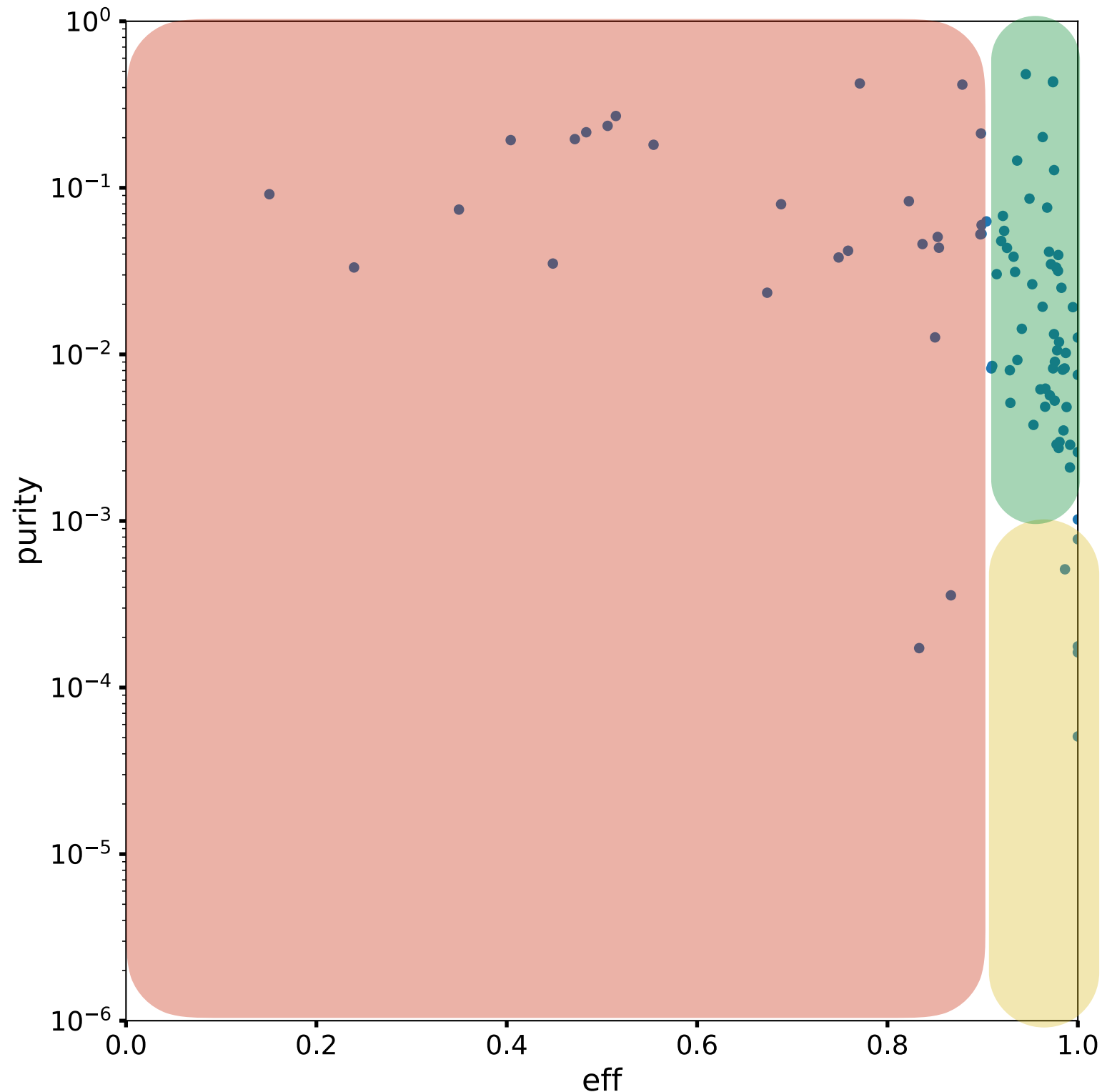
Build 90 promising layer-pairs,  
each having a Neural Network to  
select the right pairs.

# Neural Network input variables

- Hit Location variables: x, y, z
  - Cluster Info: x, y, z
    - x-y-z on the module:
      - $x = (\max(\text{ch0}) - \min(\text{ch0})) * \text{pitch\_x};$
      - $y = (\max(\text{ch1}) - \min(\text{ch1})) * \text{pitch\_y};$
      - $z = \text{module\_width}$
    - local x-y-z  $\rightarrow$  global x-y-z
      - Use rotation-matrix and translation vector
  - **In total 12 input variables.**
- Noise hits and duplicated hits are used as well.**



# Neural network performance



Most Lay-pairs achieve  
 $> 90\%$  efficiency at the cost  
of purity  $\sim 0.1\%$ .

Can perform fine-tuning for  
these handful worse-  
performed NNs

Will proceed to construct  
the graph for all events.

# Short-term focus

1. Complete full event process (including endcap and noise hits) using the NNs + GNN + CTD.
2. Deal with unknown missing hits and duplicated hits
  1. Join the efforts from traditional algorithms
3. Scale GNN model:
  1. GNN normally does not have good scalability;
  2. Active research efforts from machine learning

